

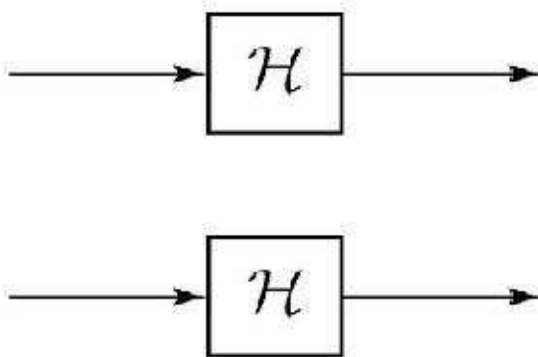
## ENSC380 Lecture 14

### Objectives:

- Find the output of LTI systems when the input (excitation) is a periodic signal

# LTI Systems

- Recall that for LTI systems, if the excitation is a complex exponential,  $e^{j2\pi ft}$  or  $e^{j2\pi fn}$ , the output is:



- Also, LTI systems are described by linear constant-coefficient differential (or difference) equations, e.g,

$$ay'(t) + y(t) = x(t)$$

- Replace  $y(t)$  and  $x(t)$  in the equation with the complex exponential, to find  $A$ :

# Periodic input

- Now consider the input to be a periodic signal  $x(t)$  and use CTFS with fundamental frequency  $f_0$  to represent it:
- For each component of  $x(t)$ ,  $X[k]e^{j2\pi(kf_0)t}$  the output is:
- Thus, the complete output is:

# Example

For the RC low pass filter below, find the output when the input signal is  $v_{in}(t) = \cos(6\pi t)$

