

## ENSC380 Lecture 8

### Objectives:

- Learn the properties of the convolution sum
- Learn how to combine systems in series and parallel
- Learn the response of LTI systems to standard excitations: unit step, complex exponential, and sinusoidal

# Convolution Properties

Convolution Sum:

$$x[n] * h[n] =$$

- **Important:**  $x[n] * \delta[n - n_0] = x[n - n_0]$
- Proof:

# Conv. Prop. (Cont.)

- Commutative:

$$x[n] * h[n] =$$

- Distributive:

$$x[n] * (h_1[n] + h_2[n]) =$$

- Associative:

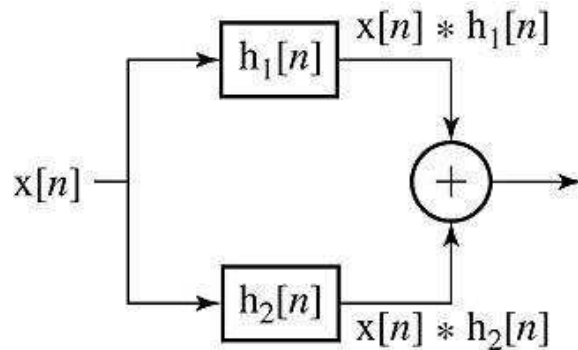
$$x[n] * (h_1[n] * h_2[n]) =$$

# System Interconnections

- Cascade (Series) connection:



- Parallel connection:



# Stability

- Recall the stability condition (BIBO)?
- How does this relate to the impulse response?

# Unit Step Response

What is the System's response to  $x[n] = u[n]$ ? (This is also called the **unit sequence response**)

# Complex Exponential Response

What is the response of the system to  $x[n] = z^n$ , where  $z$  is a complex number?

# Sinusoidal Response

What is the response of the system to  $x[n] = \cos(2\pi Fn)$ ?

- $\cos(2\pi Fn)$  can be written in terms of complex exponentials:
- Find the response of the system to each exponential and combine:
- It can be shown that the result is:

$$y[n] = \cos(2\pi Fn) \sum_{m=-\infty}^{\infty} h[m] \cos(2\pi Fm) + \sin(2\pi Fn) \sum_{m=-\infty}^{\infty} h[m] \sin(2\pi Fm)$$



# Example

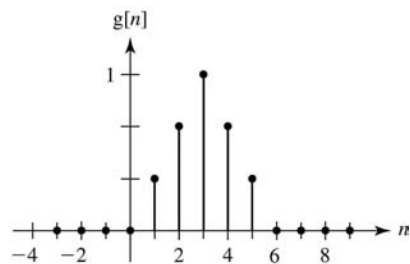
The unit sequence response to a system is given as:

$$y[n] = \left[ 5 - 4\left(\frac{4}{5}\right)^n \right] u[n]$$

Find the impulse response of the system:

# Example (Cont.)

Find the response of the system to  $x[n]$  given below:



Answer using Matlab (See page 168, Text)

