

$$f = 1592 \text{ Hz}$$

Solve using mesh analysis

$$\omega = 2\pi 1592 = 10^4 \text{ rad/s}$$

$$\therefore Z_{L_1} = j\omega L = j10^4(20 \times 10^{-3}) = j200 \Omega$$

$$= 200 \angle 90^\circ$$

$$Z_{C_1} = -j \frac{1}{\omega C} = \frac{-j}{10^4 \times 10^{-6}} = -j100 \Omega$$

$$= 100 \angle -90^\circ$$

Mesh equation =

$$V_1 = \left( R_1 - \frac{j}{\omega C} \right) I_1 + \left( \frac{-j}{\omega C} \right) I_2$$

$$10 \angle 90^\circ = (200 - j100) I_1 - j100 I_2$$

$$I_2 = 50 \text{ mA} \angle 0^\circ$$

$$\text{But } I_2 = 50 \text{ mA } \angle 0^\circ$$

$\therefore$  reduces to 1 equation  
by supermesh or pseudomesh

$$j10 = (200 - j100)I_1 - j100(0.05)$$

$$j10 + j5 = j15 = (200 - j100)I_1$$

$$I_{R_1} = I_1 = \frac{j15}{(200 - j100)} \quad \theta = \arctan\left(\frac{-100}{200}\right)$$

$$= -26.6^\circ$$

$$= \frac{15 \angle 90^\circ}{223.6 \angle -26.6^\circ}$$

$$= 67.1 \text{ mA } \angle 116.6^\circ$$

$$I_{C_1} = I_1 + I_2 = (-30 + j60) + (50) \text{ mA}$$

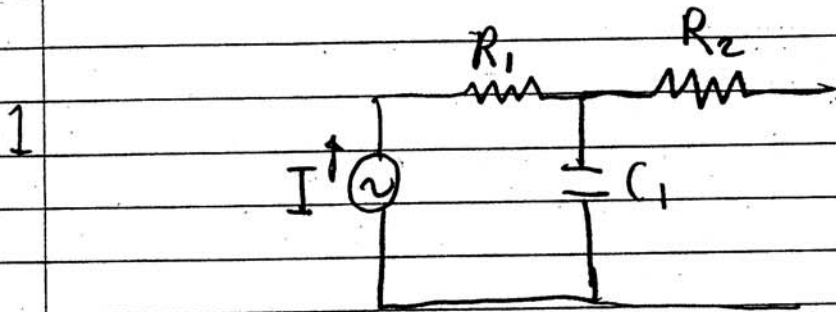
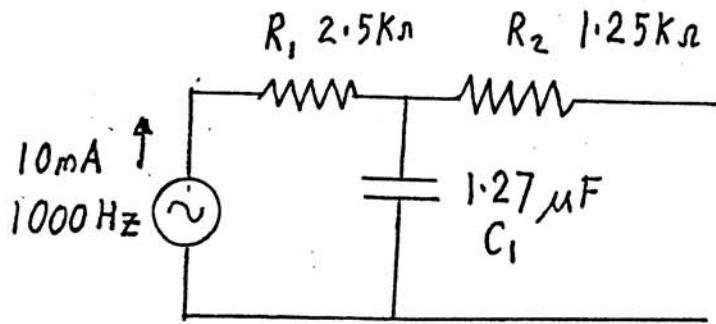
$$= (20 + j60) \text{ mA}$$

$$= 63.2 \text{ mA } \angle 71.6^\circ$$

$$\begin{aligned}V_{C_1} &= Z_{C_1} I_{C_1} \\&= 100 \angle -90^\circ 63.2 \text{ mA} \angle 71.6^\circ \\&= 6.32 \angle -18.4^\circ = (6 - j2) \text{ V}\end{aligned}$$

$$\begin{aligned}V_{R_1} &= R_1 I_1 \\&= 200 (67.1 \angle 116.6^\circ) \\&= 13.4 \angle 116.6^\circ = (-6 + j12) \text{ V}\end{aligned}$$

$$\begin{aligned}V_1 &= V_{R_1} + V_{C_1} = (-6 + j12) + (6 - j2) \\&= j10 \text{ V}\end{aligned}$$



For Thevenin want the open circuit voltage

$$V_{th} = I Z_c$$

Since power is a current source

$$V_{th} = I_1 Z_c = \frac{1}{j \omega C_1}$$

$$\omega = 2\pi 1000 = 6283 \text{ rad/s}$$

$$I_1 = 10 \text{ mA} \angle 0^\circ$$

$$Z_c = \frac{1}{j \omega C} = \frac{1}{j 6283} = \frac{1}{j 7.98 \times 10^{-3}} = -j 125 = -125 \angle -90^\circ$$

$$V_{th} = I Z_C = 10m \angle 0 \cdot 125 \angle -90$$

$$= 1.25 \angle -90 \text{ V}$$

input impedance for  $Z_{th}$

Open circuiting the  $I$

$$Z_{th} = R_2 + Z_{C1} = 1250 - j125$$

$$|Z_{th}| = \sqrt{1250^2 + 125^2} = 1256$$

$$\theta_{th} = \tan^{-1} \left( \frac{Z_I}{Z_R} \right) = \tan^{-1} \left( \frac{-125}{1250} \right) = -5.72^\circ$$

$$Z_{th} = 1256 \angle -5.72^\circ$$

(b) Norton equivalent

$$Z_N = Z_{th} = 1256 \angle -5.72$$

$$I_N = \frac{V_{th}}{Z_{th}} = \frac{1.25 \angle -90^\circ}{1256 \angle -5.72}$$

$$= 1.01 \text{ mA} \angle -84.3^\circ$$

