

# FRACTALS FOR ELECTRONIC APPLICATIONS

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PLVS RATIO  QVAM VIS



# FRACTALS

The discovery of fractals is usually bestowed upon IBM Researcher Benoit Mandelbrot in 1976. It involved calculations that could only be achieved by an intensive iteration process performed by computers...

# Fractal – “broken, fragmented, irregular”

“I coined *fractal* from the Latin adjective *fractus*. The corresponding Latin verb *frangere* means "to break" to create irregular fragments. It is therefore sensible - and how appropriate for our need ! - that, in addition to "fragmented" (as in *fraction* or *refraction*), *fractus* should also mean "irregular", both meanings being preserved in *fragment*.”

Benoit Mandelbrot : The fractal Geometry of Nature, 1982



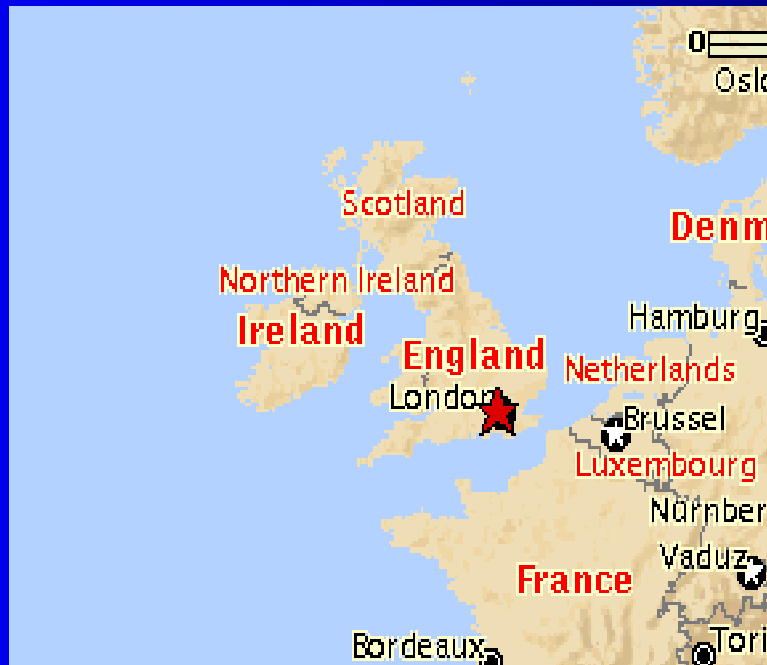
- Euclid geometry: cold and dry
- Nature: complex, irregular, fragmented

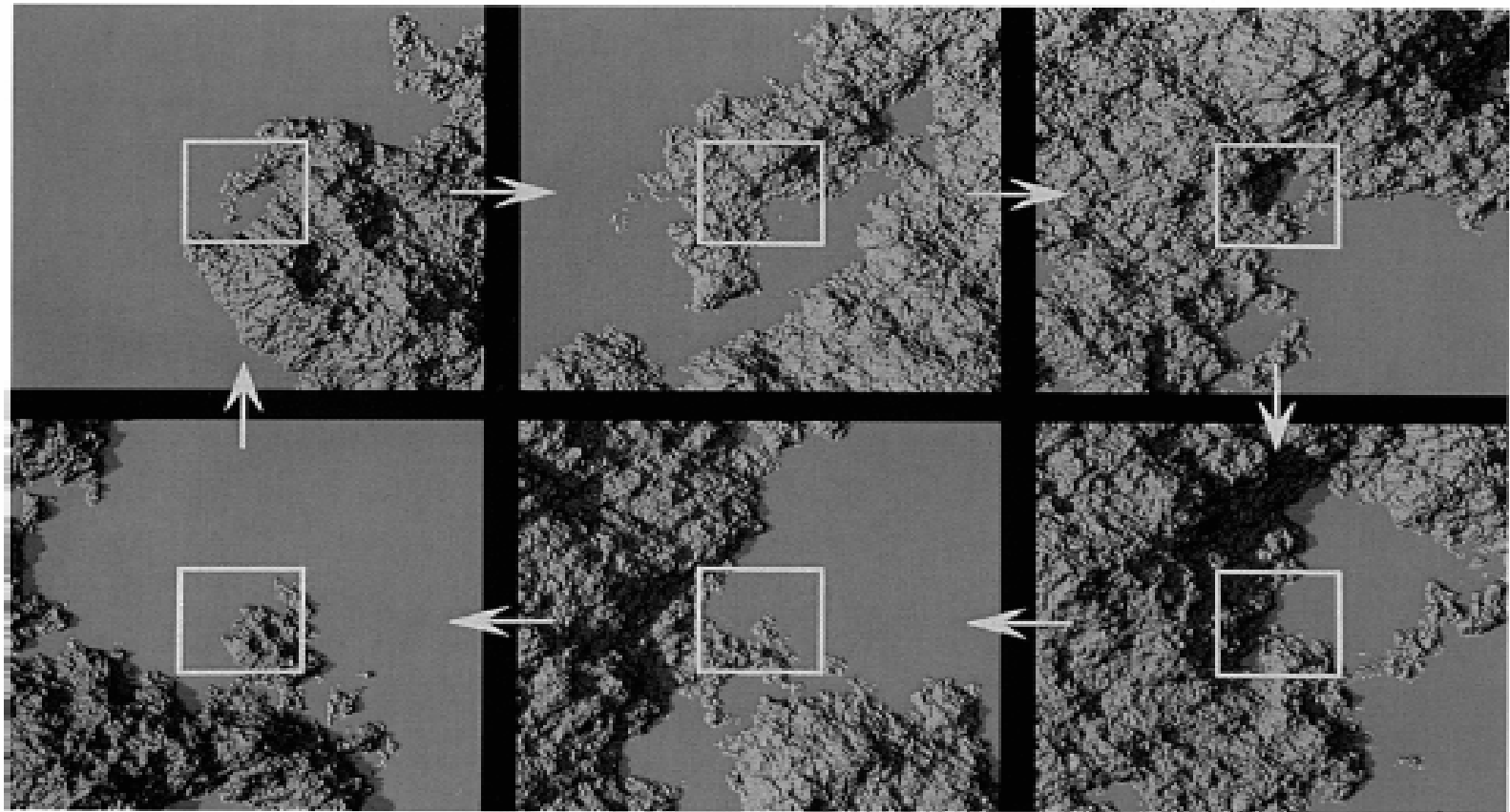
“Clouds are not spheres, mountains are not cones, coastlines are not circles, and bark is not smooth, nor does lightning travel in a straight line.” We are confronted with „rough” and „smooth” !!

# Real world fractals

A cloud, a mountain, a flower, a tree  
or a coastline...

## The coastline of Britain





Fractal Coastline (6 magnifications)

# Euclid dimension

- In Euclid geometry, dimensions of objects are defined by integer numbers.
- 0 - A point
- 1 - A curve or line
- 2 - Triangles, circles or surfaces
- 3 - Spheres, cubes and other solids

- For a square we have  $N^2$  self-similar pieces for the magnification factor of  $N$

$$\text{dimension} = \frac{\log(\text{number of self-similar pieces})}{\log(\text{magnification factor})}$$

$$= \frac{\log(N^2)}{\log N} = 2$$

For a cube we have  $N^3$  self-similar pieces

$$\text{dimension} = \frac{\log(\text{number of self-similar pieces})}{\log(\text{magnification factor})}$$

$$= \frac{\log(N^3)}{\log N} = 3$$

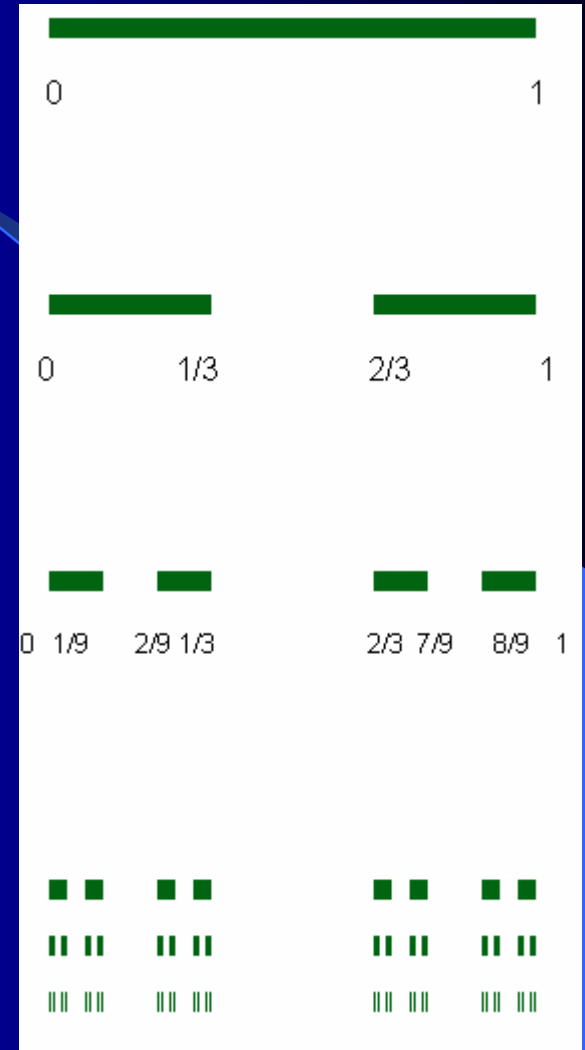
Sierpinski triangle consists of three self-similar pieces with magnification factor 2 each

$$\text{dimension} = \frac{\log 3}{\log 2} = 1.58$$



# Example: Cantor Set

- The oldest, simplest, most famous fractal
- 1 We begin with the closed interval  $[0, 1]$ .
- 2 Now we remove the open interval  $(1/3, 2/3)$ ; leaving two closed intervals behind.
- 3 We repeat the procedure, removing the "open middle third" of each of these intervals
- 4 And continue infinitely.
- Fractal dimension:  
 $D = \log 2 / \log 3 = 0.63\dots$
- Uncountable points, zero length

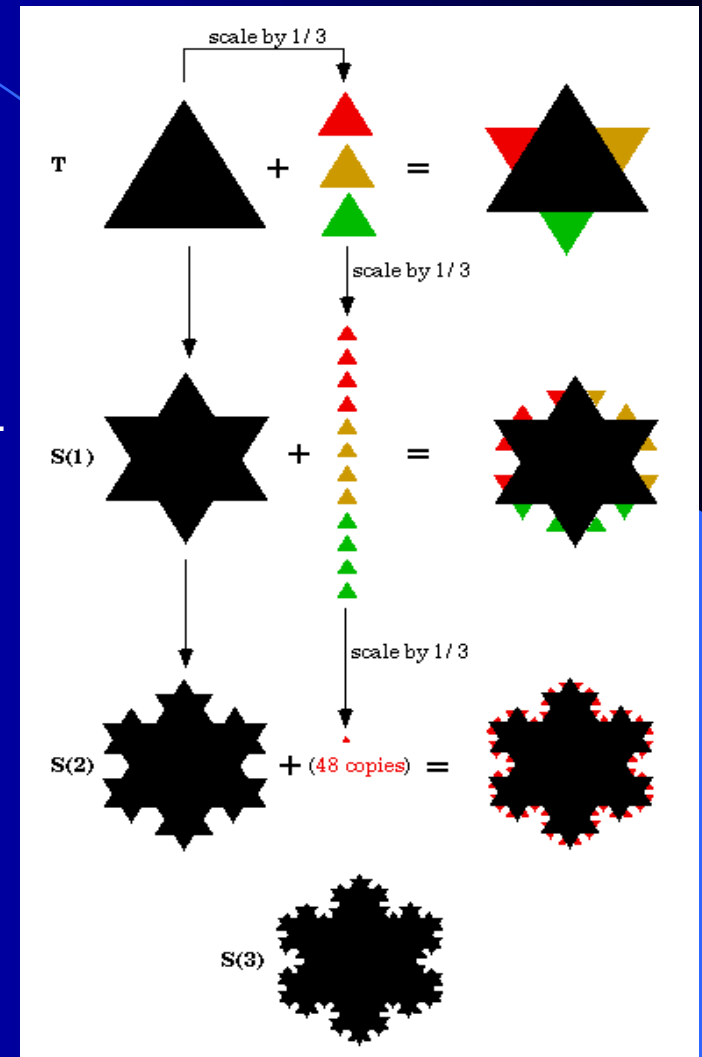




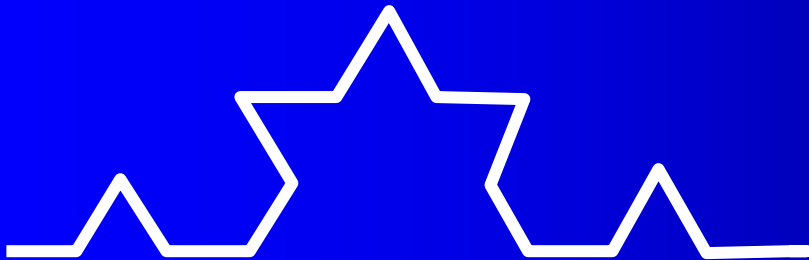


# Helge von Koch Snowflake

- Step One.  
Start with a large equilateral triangle.
- Step Two.  
Make a Star.
  1. Divide one side of the triangle into three parts and remove the middle section.
  2. Replace it with two lines the same length as the section you removed.
  3. Do this to all three sides of the triangle.
- Repeat this process infinitely.
- The snowflake has a finite area bounded by a perimeter of infinite length!



# Scaling/dimension of the von Koch curve



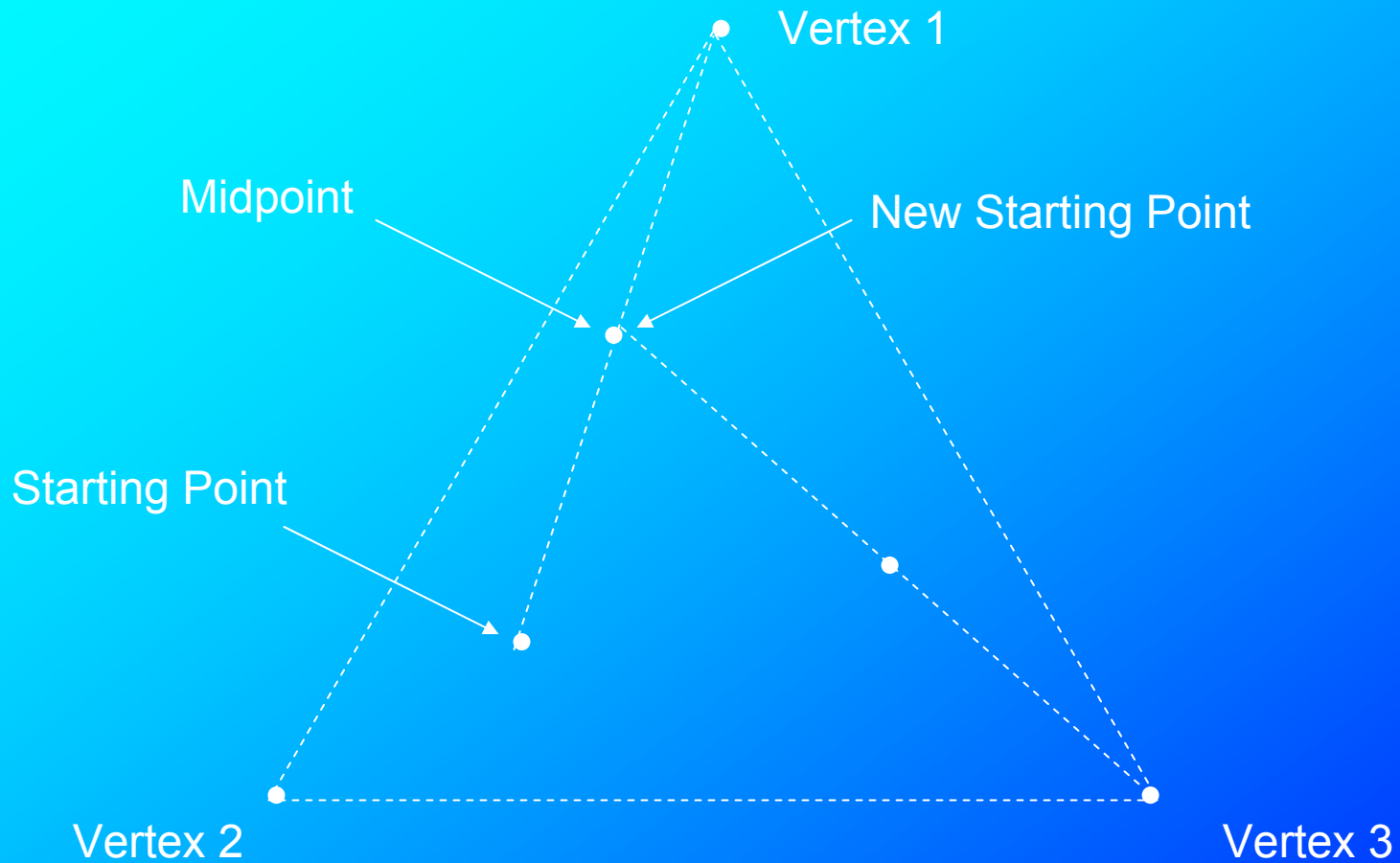
- Scale by 3 – need four self-similar pieces
- $D = \log 4 / \log 3 = 1.26$

# Sierpiński Fractals

- Named for Polish mathematician Waclaw Sierpinski
- Involve basic geometric polygons



# Sierpinski Chaos Game

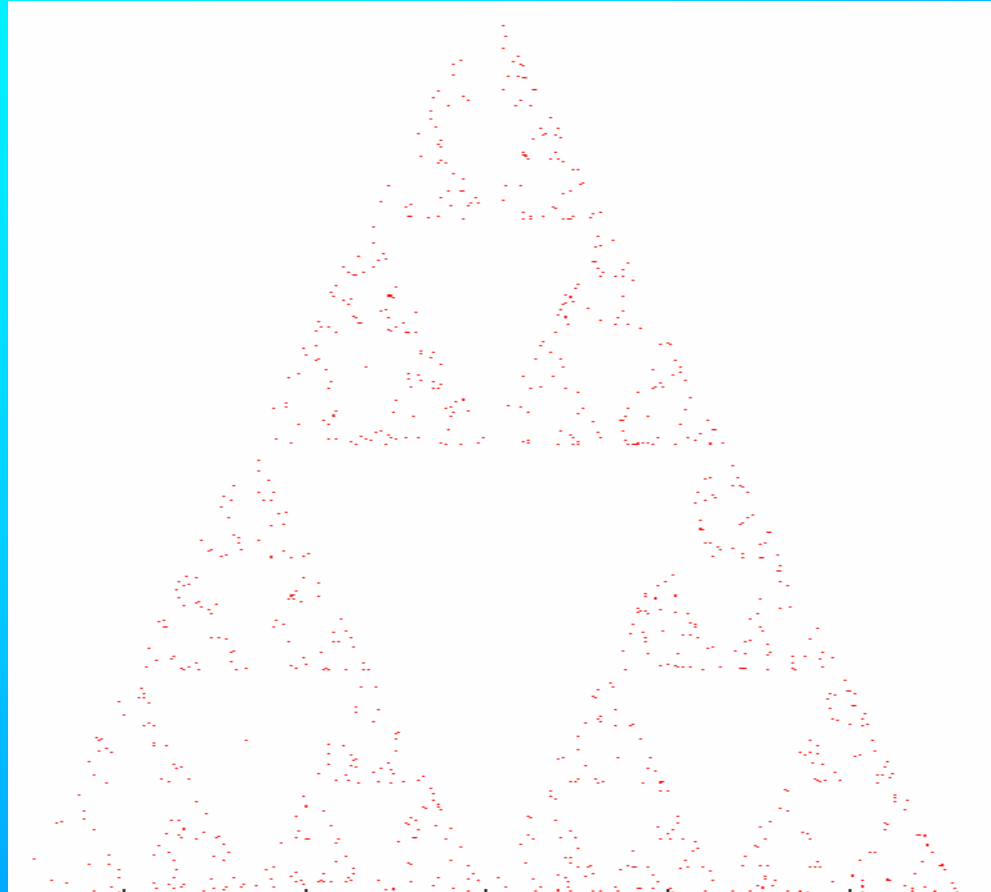


# Sierpinski Chaos Game



● 100 pts

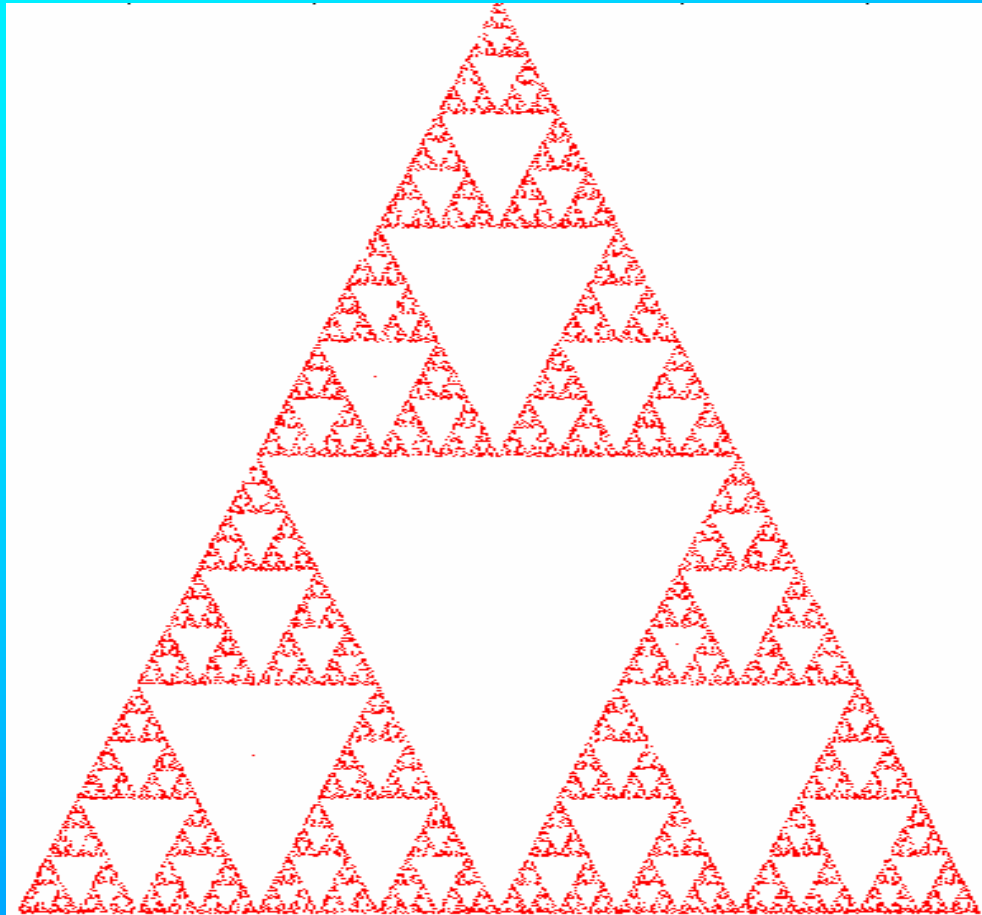
# Sierpinski Chaos Game



● 1000 pts

# Sierpinski Chaos Game

Fractal dimension = 1.8175...

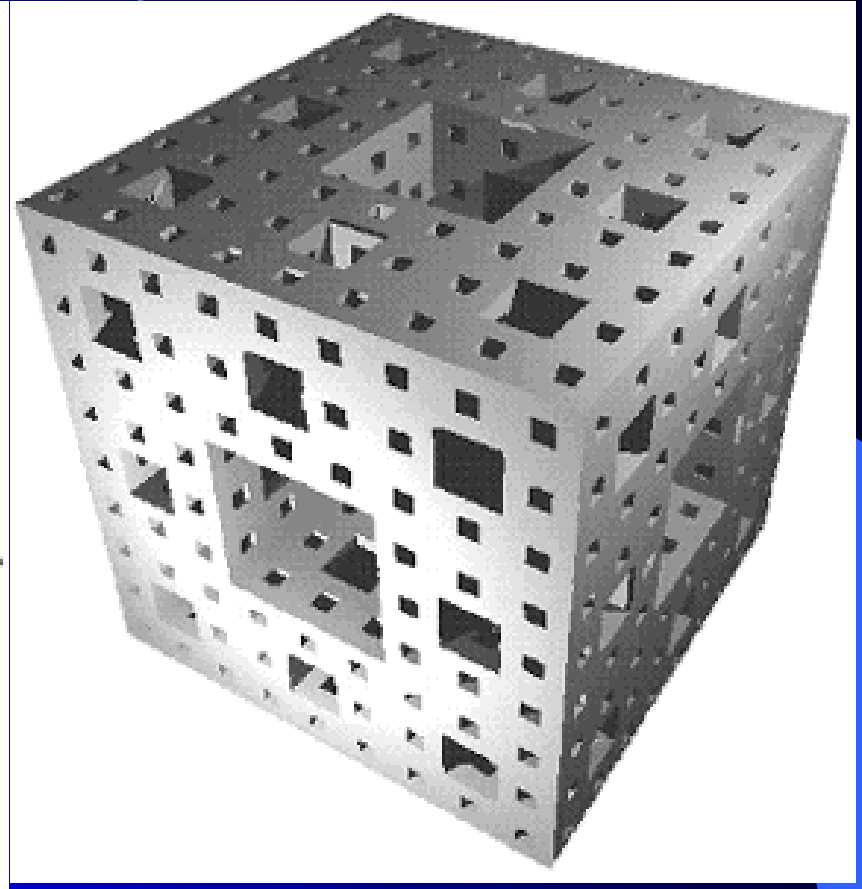
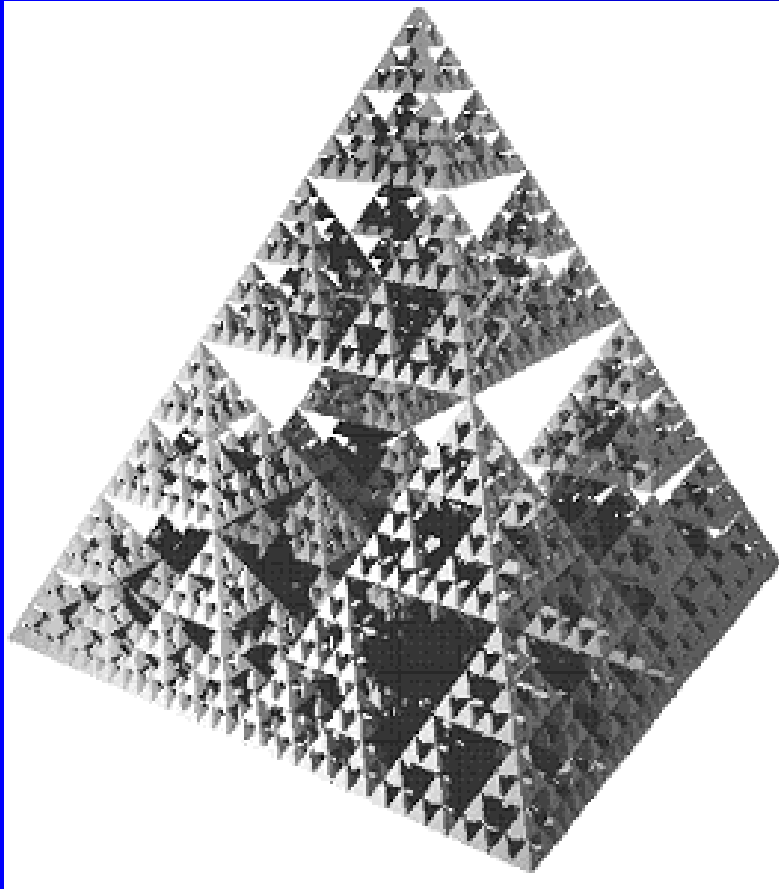


● 20000 pts

- Most important properties for applications
- Fractal structures embedded in 2D have  
finite area but infinite perimeter
- Fractal structures embedded in 3D have  
finite volume but infinite surface



# In 3-D



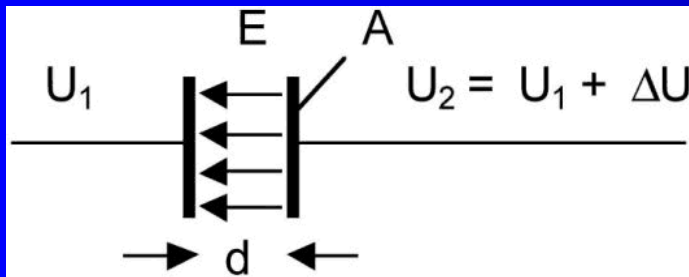
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- **These "broken curves" have been used to explain naturally-occurring phenomenon such as lightning, galactic clusters and clouds. Many computer-image compression schemes are based on fractals. Until recently, however, there have been few hardware applications of fractal geometry.**


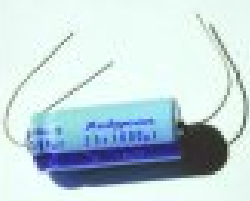



# Physical relations for capacitors

Both electrodes have a surface  $A$  (in  $\text{m}^2$ ) separated by distance  $d$  (in  $\text{m}$ ). The applied voltage  $\Delta U$  (in Volt) creates an electric field  $E = \Delta U/d$  storing the electrical energy. Capacitance  $C$  in Farad (F) and stored energy  $J$  in Ws is:



$$C = \epsilon_0 \cdot \epsilon_r \frac{A}{d} \quad J = \frac{1}{2} C \cdot \Delta U^2$$

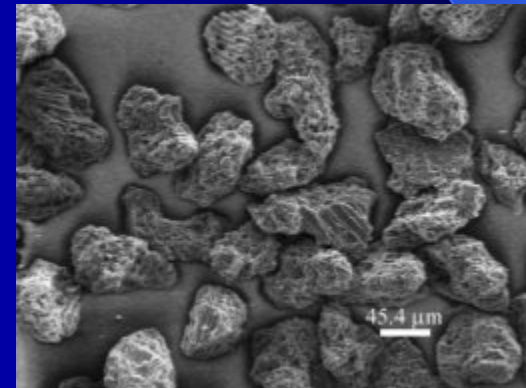
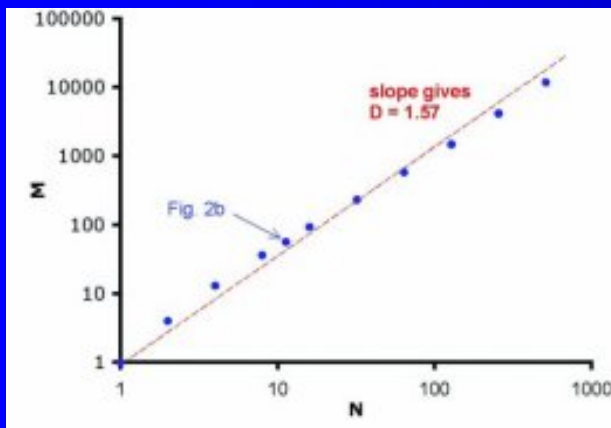
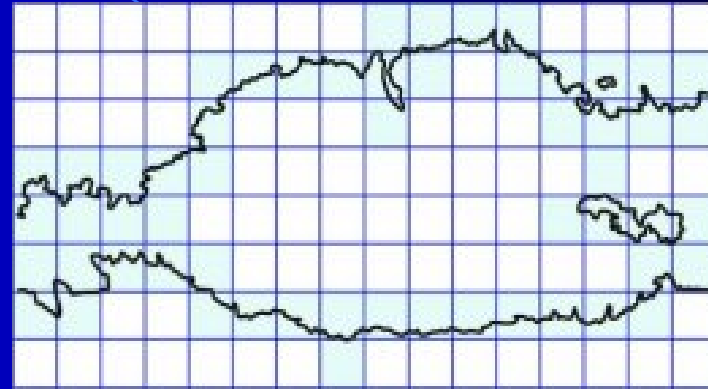
where  $\epsilon_r$  (e.g. 1 for vacuum or 81 for water) is the relative dielectric constant which depends on the material placed between the two electrodes and  $\epsilon_0 = 8.85 \cdot 10^{-12} \text{ F/m}$  is a fundamental constant.

Capacitance in Farad	1000	$1 \cdot 10^{-3}$	$1 \cdot 10^{-6}$	$1 \cdot 10^{-9}$	$1 \cdot 10^{-12}$
Example	 <p>supercapacitor with 1500 F, max. 2.5 V (positive electrode left)</p>	 <p>electrolyte capacitor with 1000 mF, max. 25 V (positive electrode left)</p>	 <p>electrolyte capacitor with 10 mF, max. 35 V (bent wire is positive electrode)</p>	 <p>rolled capacitor with 51 nF, max. 63 V</p>	 <p>plate capacitors with 50 pF. Left: an element from an old vacuum-tube radio in the form of two plates rolled to a cylinder, max. 450 V. Right: modern ceramic element, max. 100 V)</p>
Energy Stored	Watt hours (Wh)	several Ws (Ws)	milli-Ws = $10^{-3}$ Ws (mWs)	milli-Ws = $10^{-3}$ Ws (mWs)	micro-Ws = $10^{-6}$ Ws (mWs)
Applications	Novel applications in power electronics: e.g. in cars, for replacing batteries in consumer electronics	Power supply units	Low frequency technology: general electronics, e.g. audio amplifiers	Low frequency technology: general electronics, e.g. audio amplifiers	High frequency technology: e.g. radio, TV, PC

# How to create capacitors with larger $C$ ?

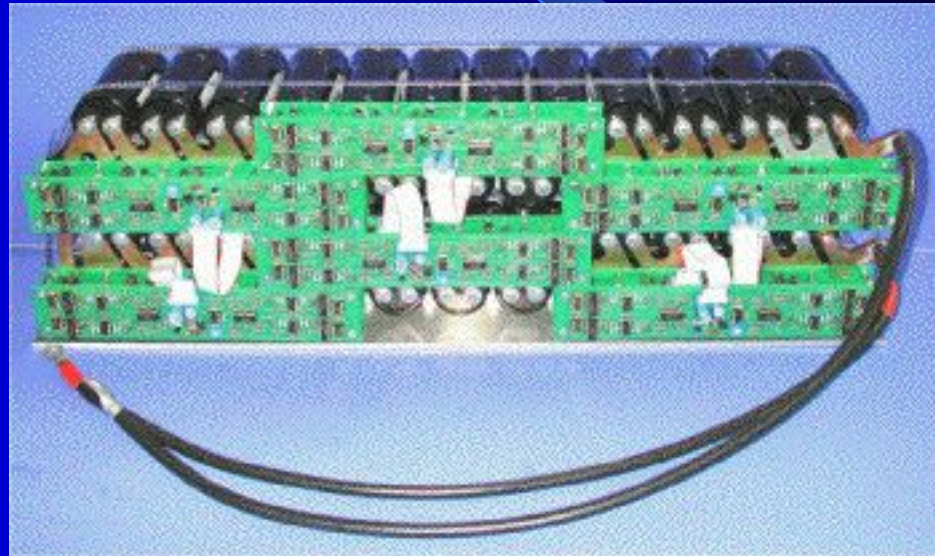
- Create capacitors with very large areas  $A$  – technologies to create fractal-type surfaces
- Use designs taking advantage of lateral capacitance in integrated circuits

Electrochemically modified glassy carbon is a promising material to be used in electrochemical capacitors. Oxidation of the surface of a glassy carbon electrode results in a porous layer with very large capacitance and fairly low internal resistance when using an aqueous electrolyte.



- Paul Scherrer Institute in Villigen, Switzerland - Rüdiger Kötz and his group have developed an electrode in collaboration with the Swiss company *Montena* (*Maxwell*).

- a) Micrograph of a cross section through a supercapacitor electrode. The white stripe is a part of the 30  $\mu\text{m}$  thick metallic carrier-foil (total foil is 0.1 m wide, 2 m long). On both sides carbon particles provide a complex fractal surface responsible for the high capacity. The space taken by the green resin used to fix the delicate carbon structure before cutting and to provide a good contrast for imaging is normally filled with the electrolyte (an organic solvent containing salt ions).
- b) Borderline of the cross section through the electrode surface in (a) to be analyzed by the box-counting procedure, illustrated for a tiling with 128 squares:  $M = 56$  squares (filled with light blue colour) are necessary to cover the borderline. Their side lengths are  $N = 11.3$  (square root of 128) times smaller than the length scale of the whole picture.
- c) The box-counting procedure is repeated with a computer program for different  $N$ . The average fractal dimension of the borderline is the gradient of the straight line approximating the measured points in this  $\text{Log}(M)$  over  $\text{Log}(N)$  plot, giving  $D = 1.6$ . This same dimension was measured in the length interval covering nearly 3 decades between 0.6 mm (length of micrograph in Figs 2a, b) and about 1  $\mu\text{m}$  (fine structure in Fig. 2d).
- d) Carbon particles as seen with an electron microscope show roughness also in the 1  $\mu\text{m}$  scale. It is assumed that the above indicated fractal dimension  $D$  holds over the entire range of 8 decades between the macroscopic scale (i.e. the geometric size of the order of 0.1 m) and the microscopic scale (i.e. the micropores in the order of 1 nm =  $1 \cdot 10^{-9}$  m). The electrode surface is therefore multiplied by  $10^{8 \cdot 0.6}$  or about 60'000 when compared to the normal two-dimensional surface of 0.2  $\text{m}^2$ .



- *800 F boostcap by montena SA utilizing PSI electrode.*
- *Capacitor module with 2 x 24 capacitors resulting in 60 V , 60 F with an overall internal resistance of < 20 mOhm.*





- Supercapacitor module for HY-LIGHT.  
Capacitance: 29 F  
Power: 30 - 45 kW for 20 - 15 sec ; Weight: 53 kg
- HY-LIGHT accelerates to 100km/h in 12 seconds

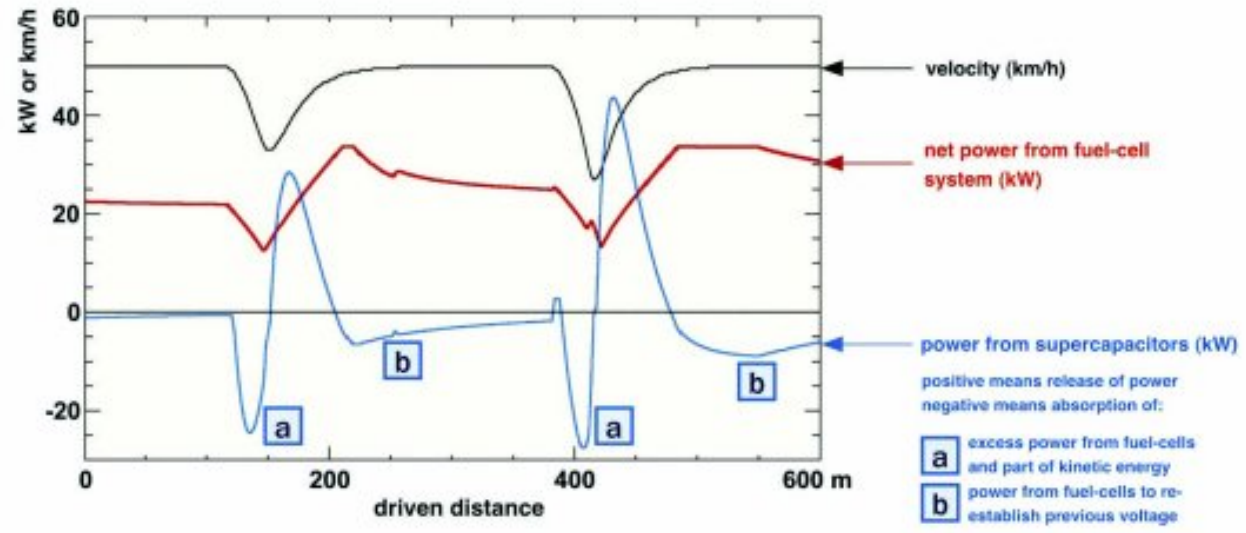
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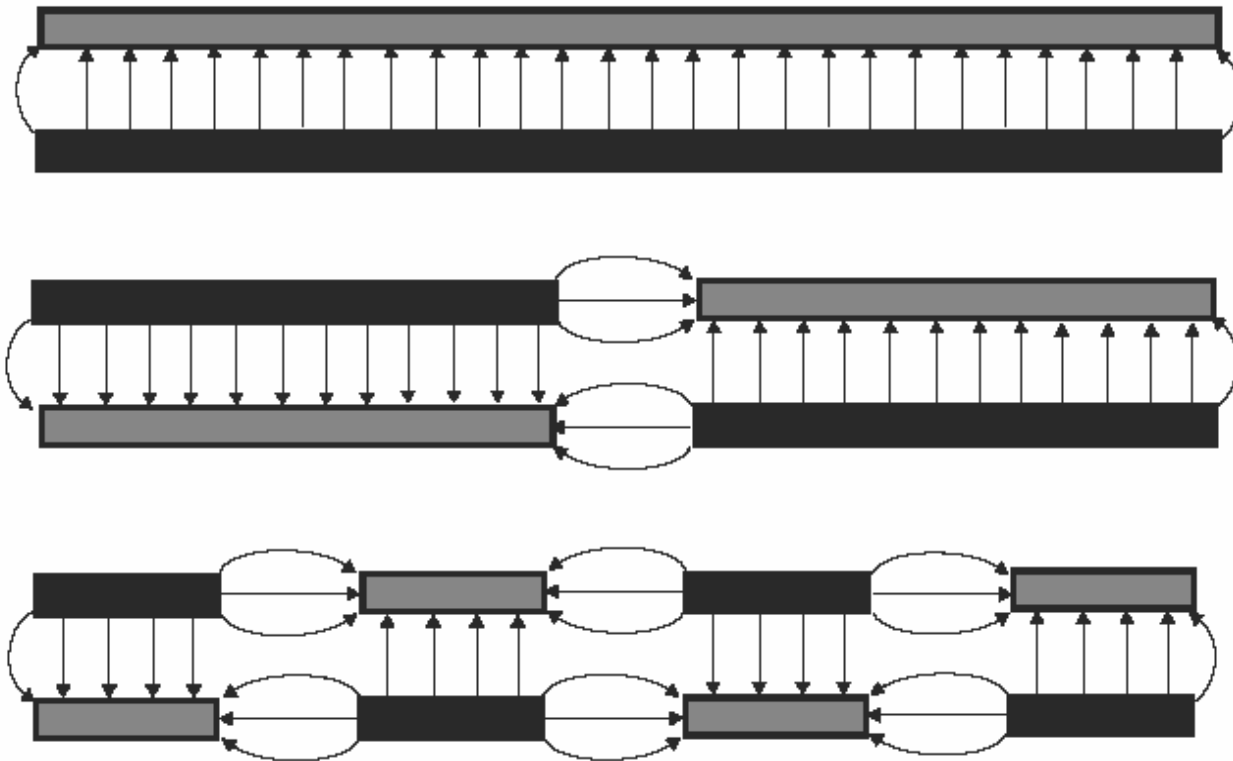
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# Vertical vs. Lateral Flux

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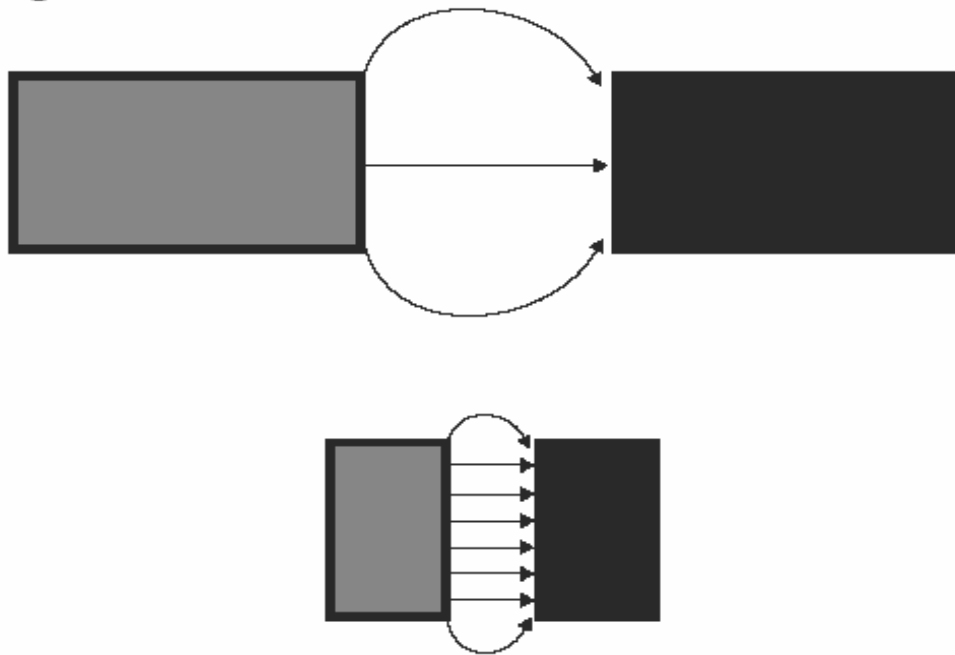
- Lateral flux increases the total amount of capacitance.



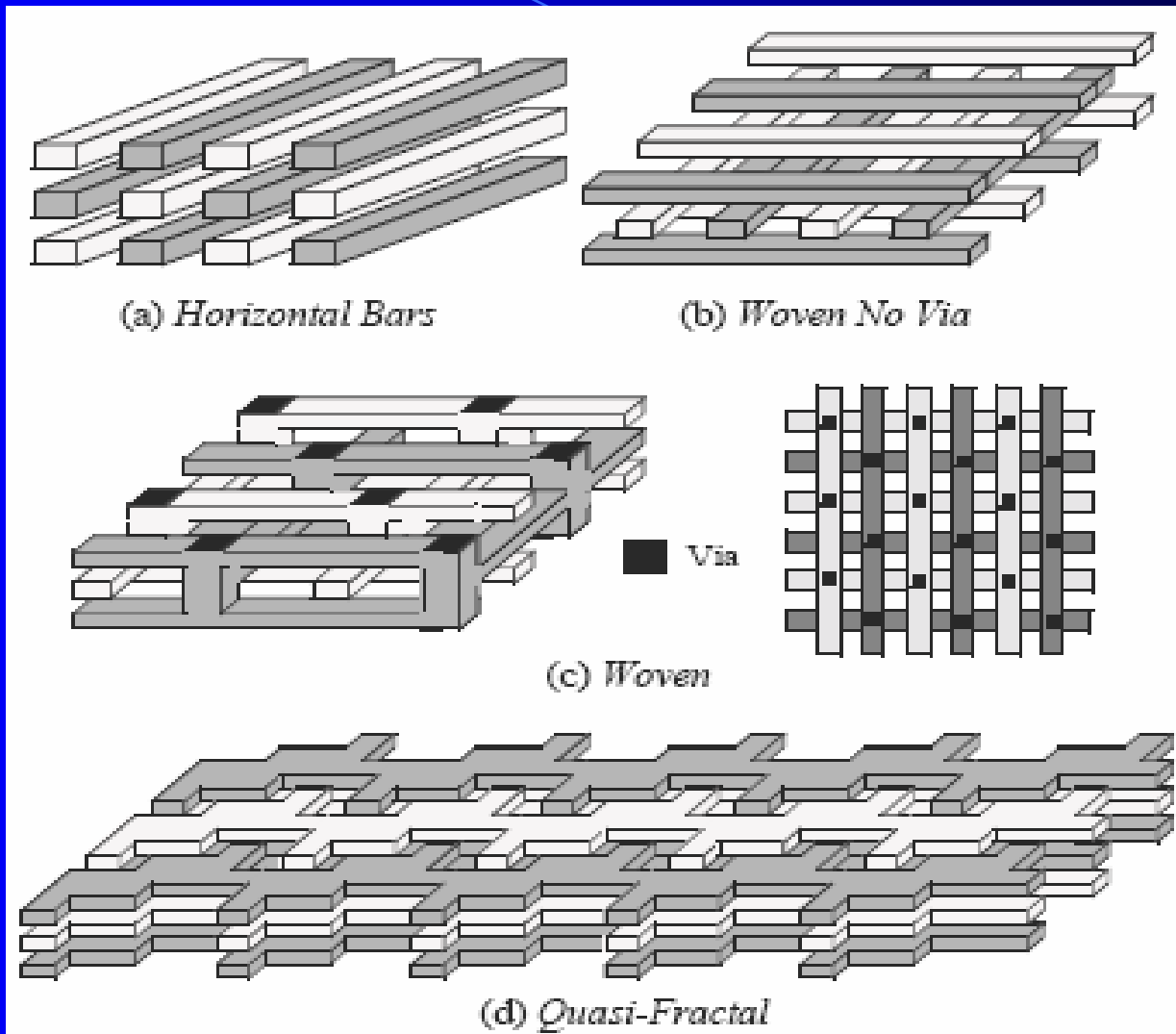
# Scaling

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- Unlike conventional parallel-plate structures, the capacitance per unit area increases as the process technologies scale.



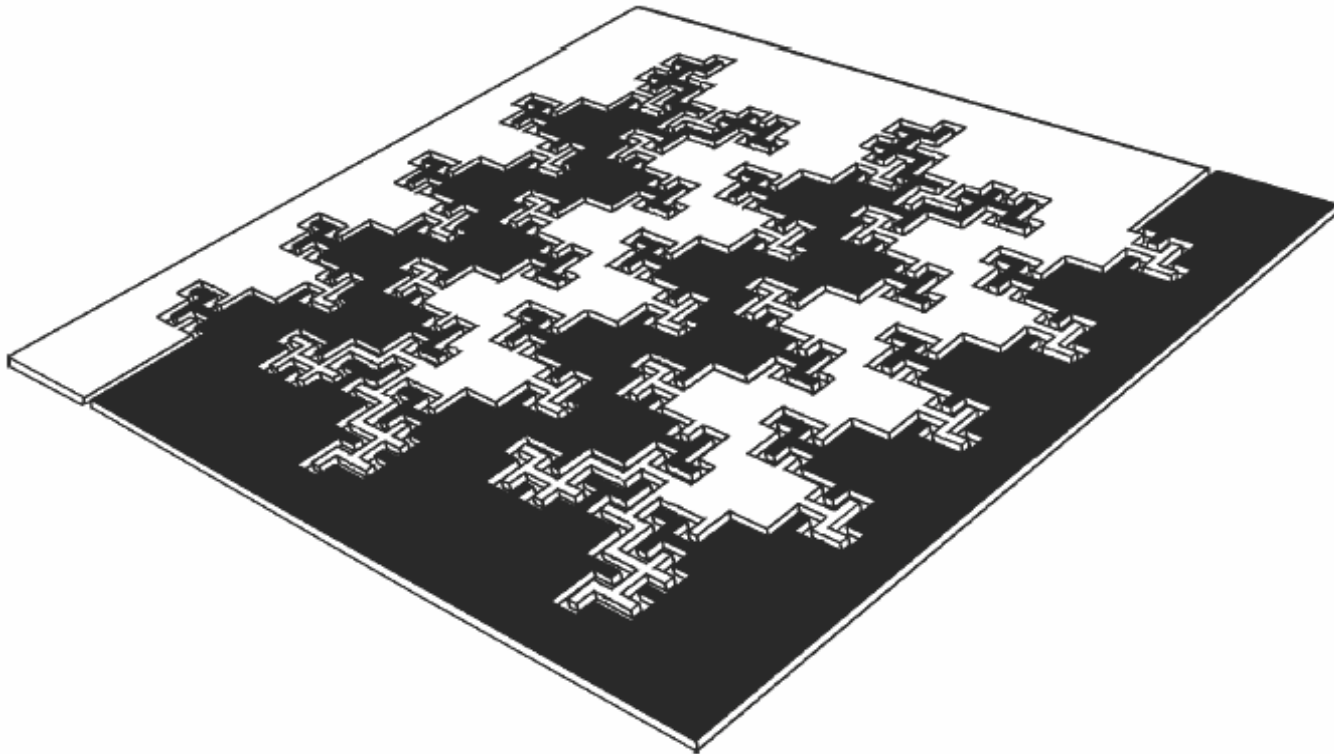
# Manhattan capacitor structures



# Fractal Capacitor

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- Quasi fractal geometries can be utilized to increase capacitance per unit area.



3-D representation of a fractal capacitor using a single metal layer.

# Capacitance Estimation

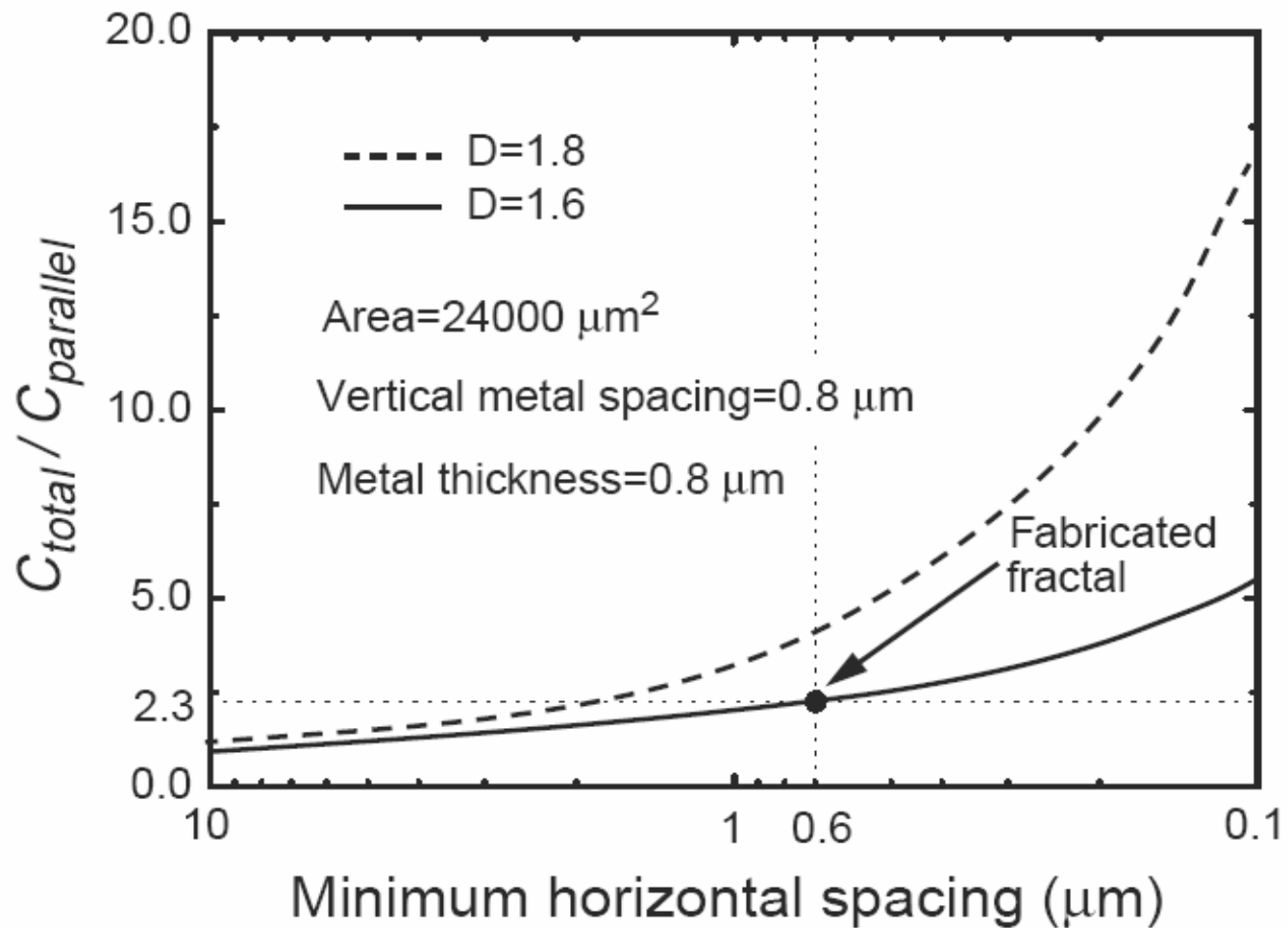
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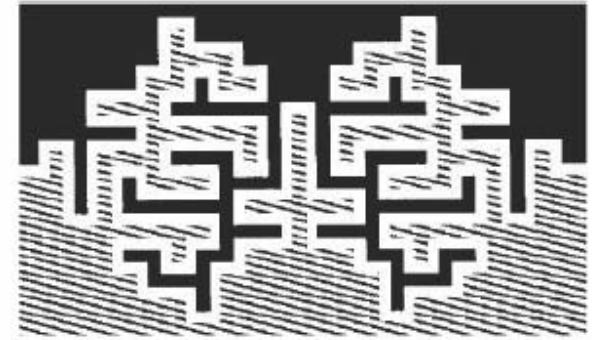
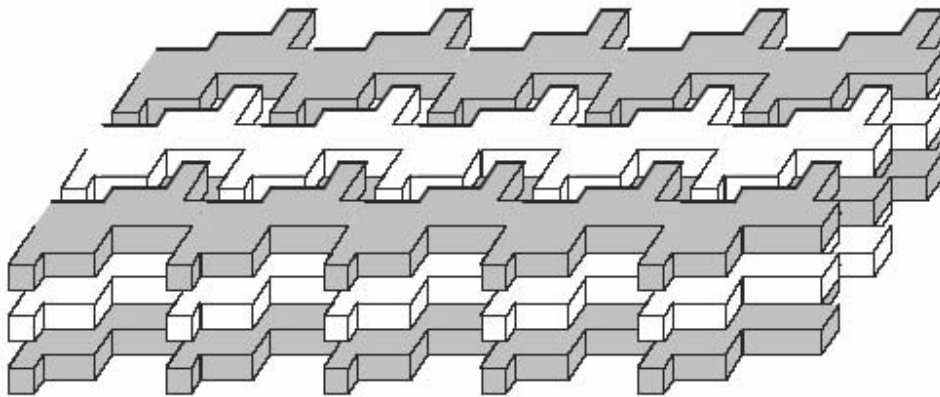
$$C_{lateral} = K \frac{(\sqrt{A})^D}{(w + s)^{D-1}} \times t$$

- $w$ : Minimum width of the metal.
- $s$ : Minimum spacing between two adjacent strips.
- $A$ : Area of the fractal capacitance.
- $t$ : Thickness of the metal layers.
- $K$ : Proportionality factor that depends on the family of fractals being used.
- $D$ : Fractal dimension.



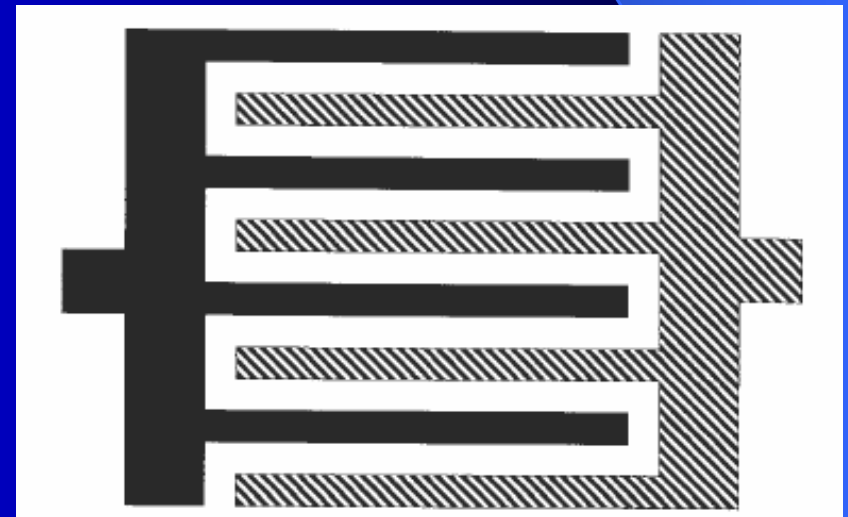
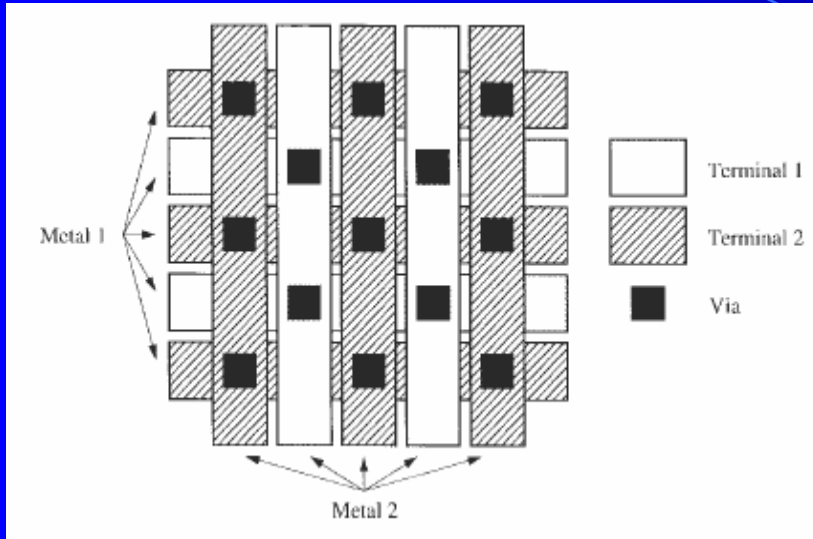
# Boost Factor vs. Lateral Spacing





- Quasi-fractal structures maximize periphery to increase field usage,
- Have strong vertical *and* lateral components,
- Time consuming to generate and simulate,
- Look beautiful !

[Samavati, Hajimiri, Shahani, Nasserbakht, and Lee, ISSCC 1998]

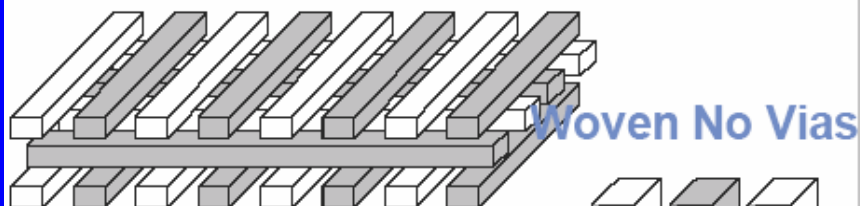
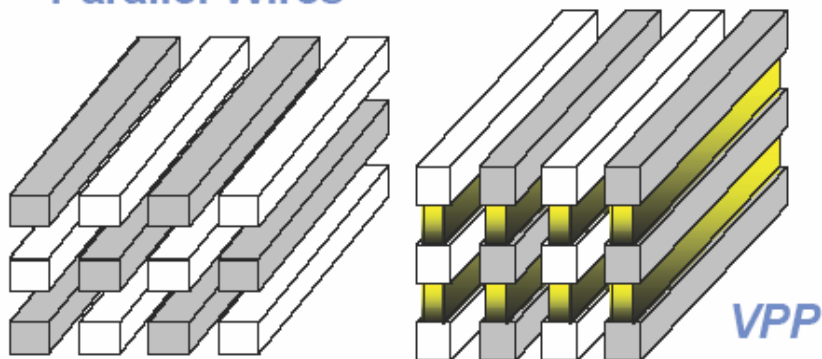


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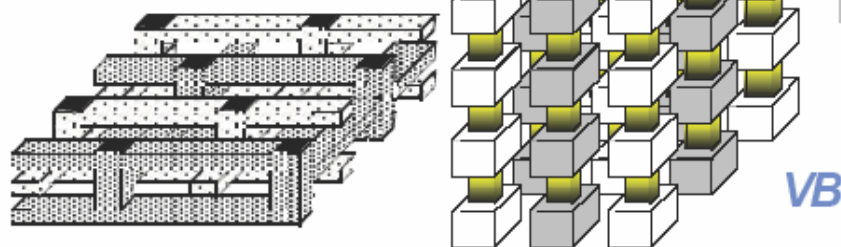
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# Capacitance density comparison

Parallel Wires



Woven



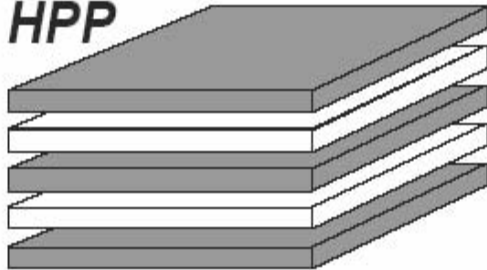
	% TL1	% TL2
Woven	37.0%	52.7%
Woven no Vias	28.3%	40.3%
Parallel Wires	28.3%	40.3%
Quasi-Fractal	17.9%	25.5%
Horizontal PP	0.8%	1.1%
Vertical PP	49.6%	70.7%
Vertical Bars	63.7%	90.8%

[Aparicio and Hajimiri, JSSC March 2002]

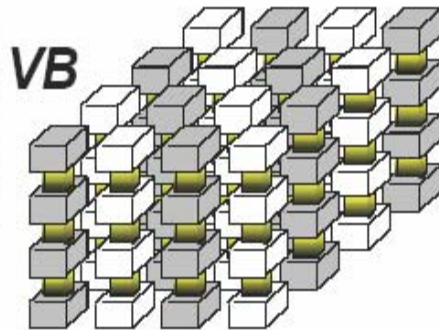


## Measurement Summary

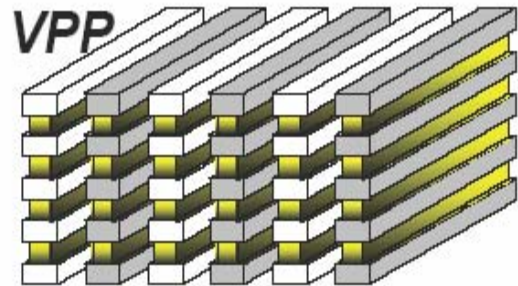
**HPP**



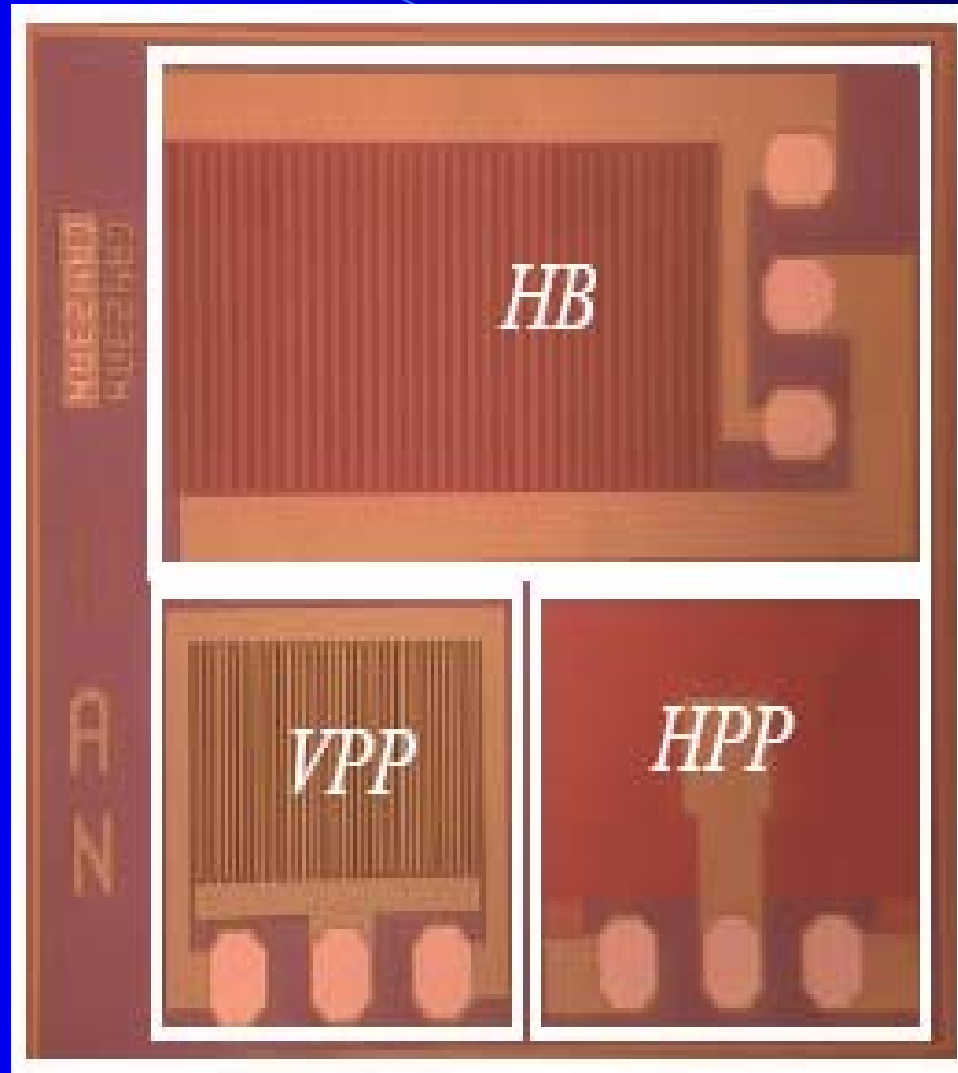
**VB**



**VPP**



	<b>HPP</b>	<b>VB</b>	<b>VPP</b>	MIM 0.18 $\mu$
Average Cap. [pF]	1.095	1.076	1.013	1.057
Cap. Density [aF/ $\mu\text{m}^2$ ]	203.6	1281.3	1512.2	1100
Cap. Enhancement	1	<b>6.29</b>	<b>7.43</b>	<b>5.40</b>
$f_{\text{res}}$ [GHz]	21	<b>37.1</b>	<b>40 &lt;</b>	<b>11</b>
Q (Measured) @1GHz	63.8	48.7	83.2	95



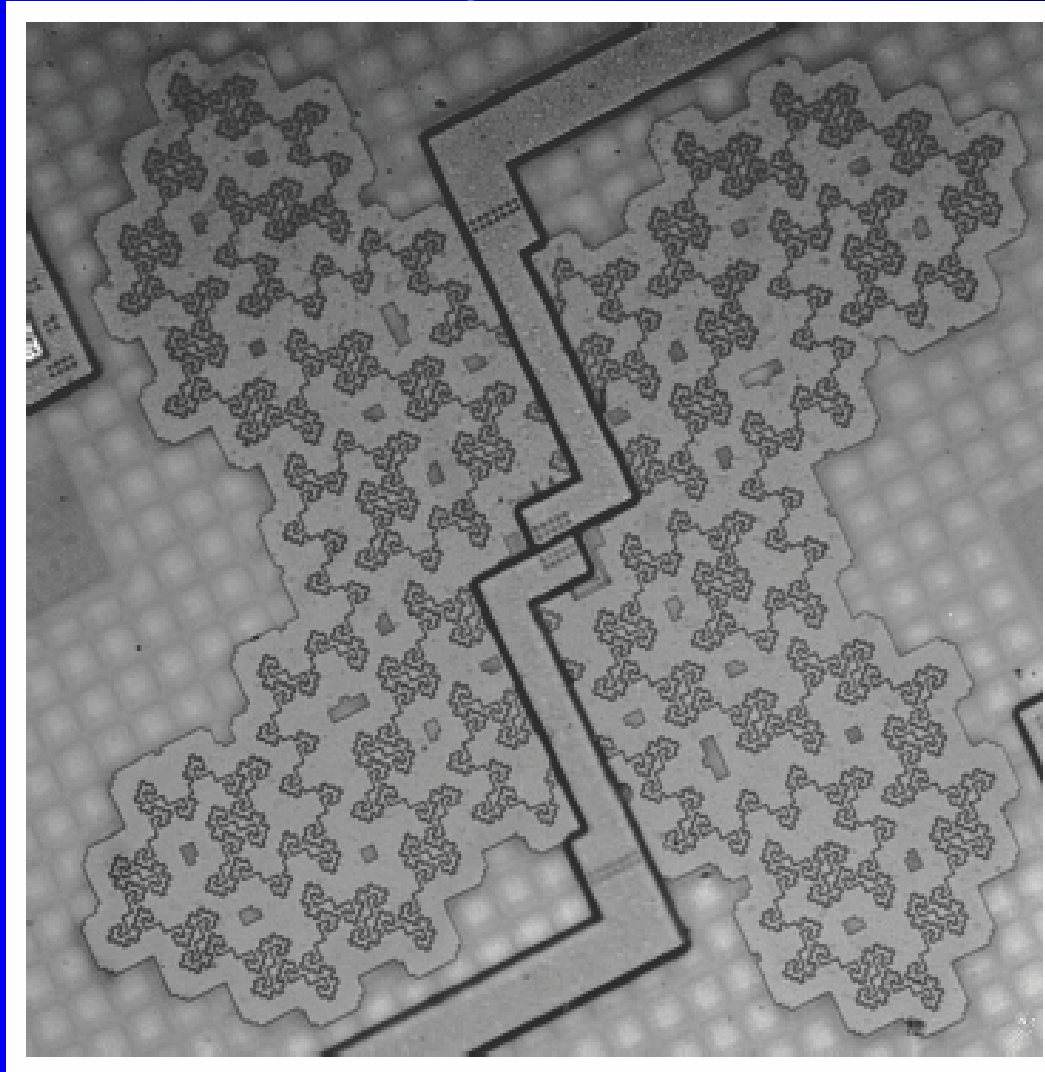
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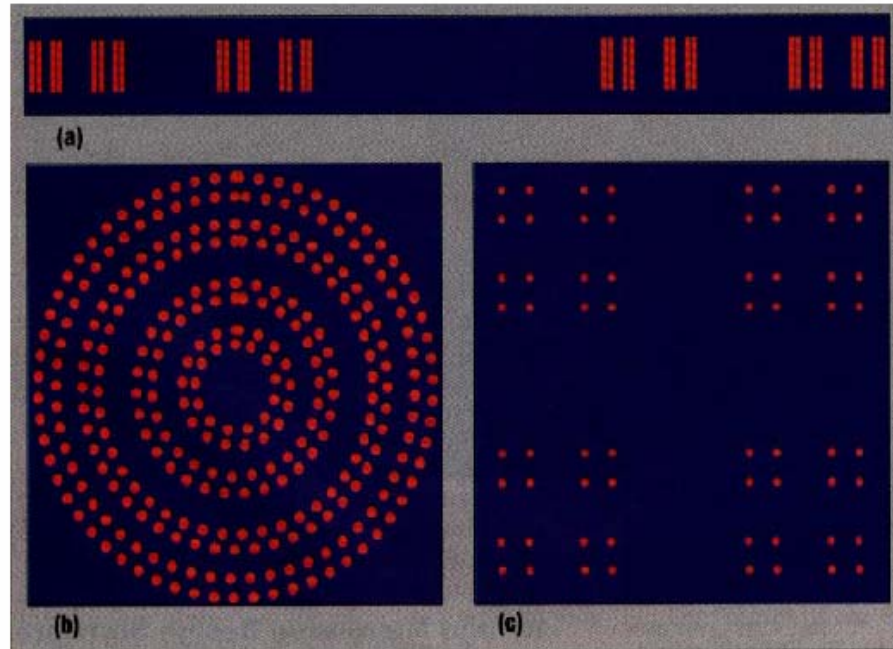
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# Open problems

- Theoretical issue: How to calculate capacitance in a „finite” fractal structure?
- Technological issues: Improve materials, find better structures

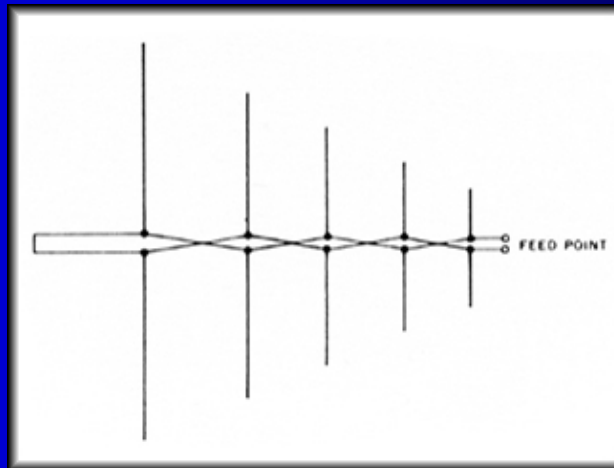
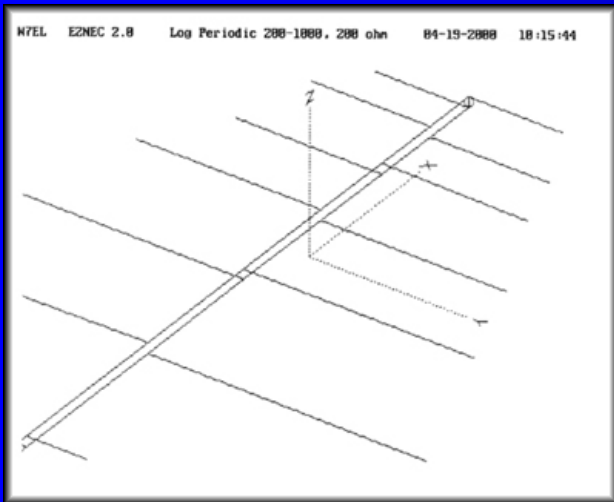
# Fractal antenna arrays



**(a)** Cantor linear array   **(b)** Cantor ring array   **(c)** Sierpinski carpet planar array

**fractal antenna** is an antenna that uses a self-similar design to maximize the length, or increase the perimeter (on inside sections or the outer structure), of material that can receive or transmit electromagnetic signals within a given total surface area. For this reason, fractal antennas are very compact, are multiband or wideband, and have useful applications in cellular telephone and microwave communications. Fractal antenna response differs markedly from traditional antenna designs, in that it is capable of operating optimally at many different frequencies simultaneously. Normally standard antennae have to be "cut" for the frequency for which they are to be used—and thus the standard antennae only optimally work at that frequency. This makes the fractal antenna an excellent design for wideband applications.

- The first fractal antennas were arrays, and not recognized initially as having self similarity as their attribute. Log-periodic antennas are arrays, around since the 1950's (invented by Isbell and DuHamel), that are such fractal antennas. They are a common form used in TV antennas, and are arrow-head in shape. Antenna elements made from self similar shapes were first done by Nathan Cohen, a professor at Boston University, in 1988. Most allusions to fractal antennas make reference to these 'fractal element antennas'.

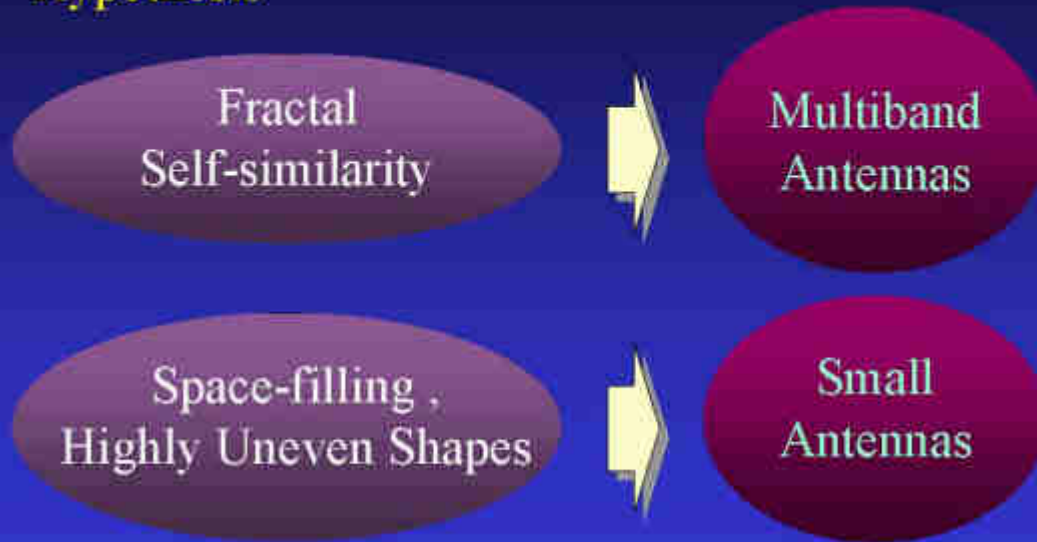


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## *Why Fractal Antennas ?*

### Hypothesis



# Which Fractals and Why?

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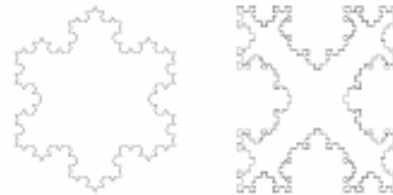
## Dipoles

Minimize Heights  
Increase Input Impedance



## Loops

Minimize Size  
Increase Input Impedance



## Dipoles

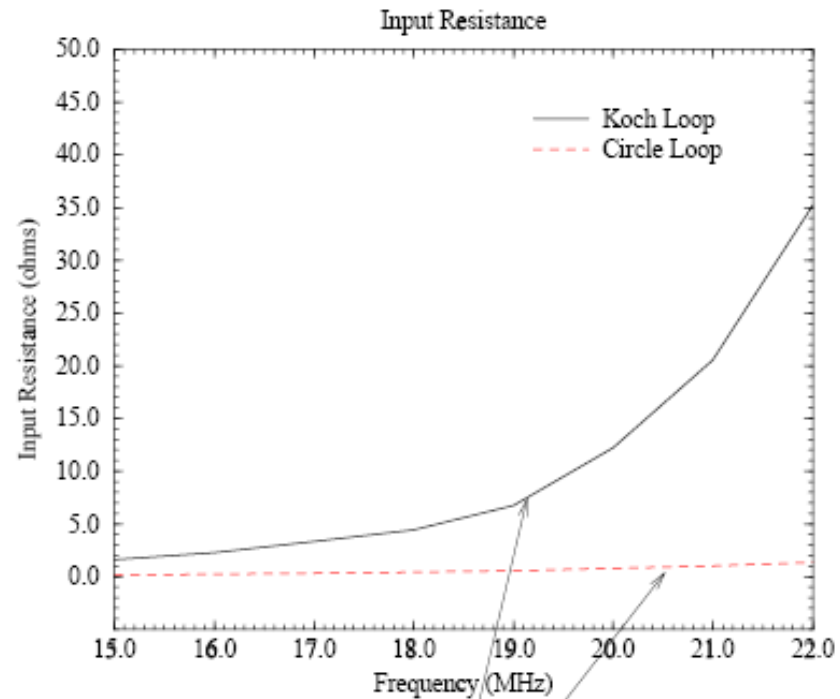
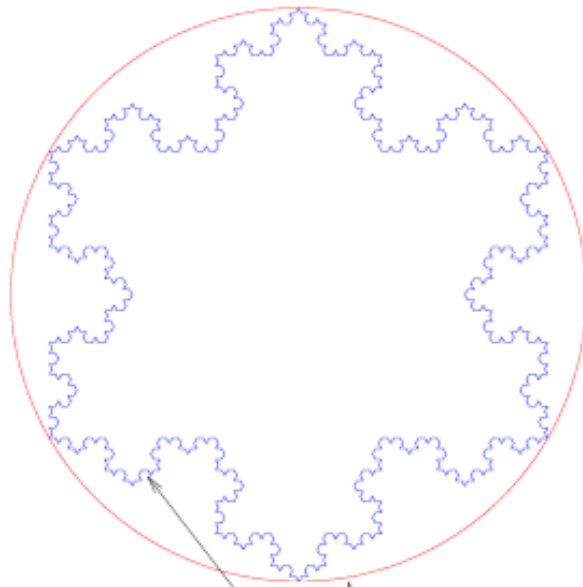
Multiband



# Small Fractal Loop Antennas

Main Benefit: Increased Input Impedance

Koch Loop vs. Circular Loop

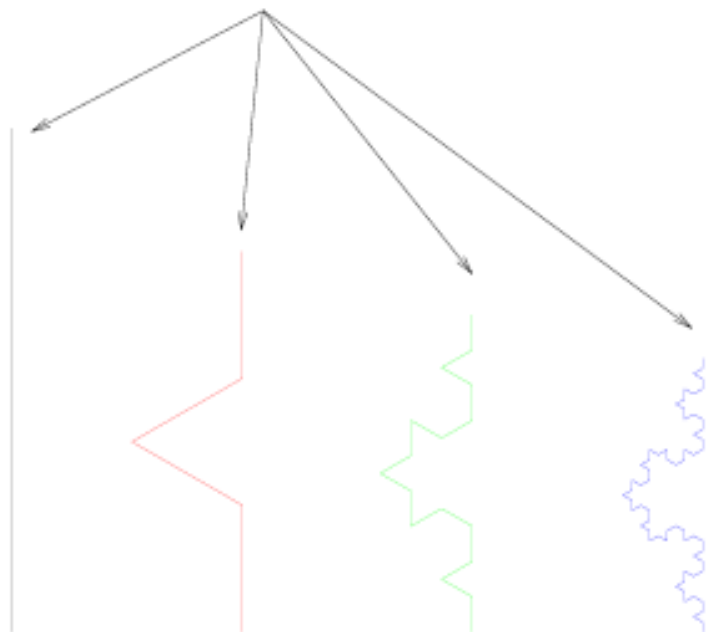


Both loops take up the same volume  
But, the input impedance of the fractal loop is higher





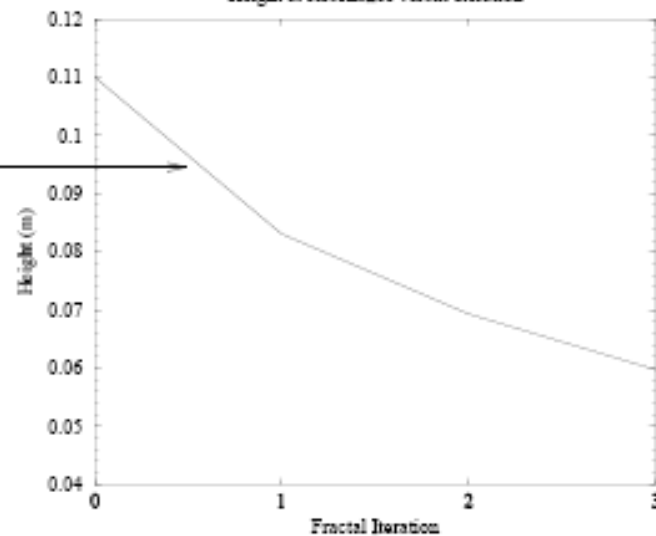
Decreasing Height for Resonant Dipoles



However, Total Length Increases

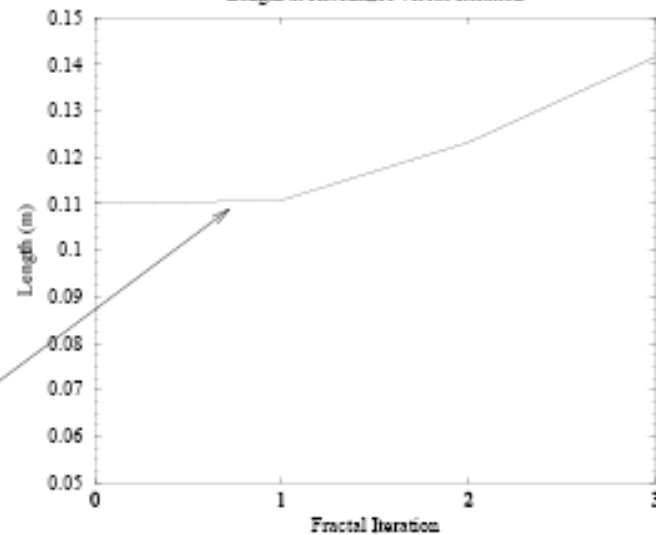
Koch Monopole

Height at Resonance versus Iteration

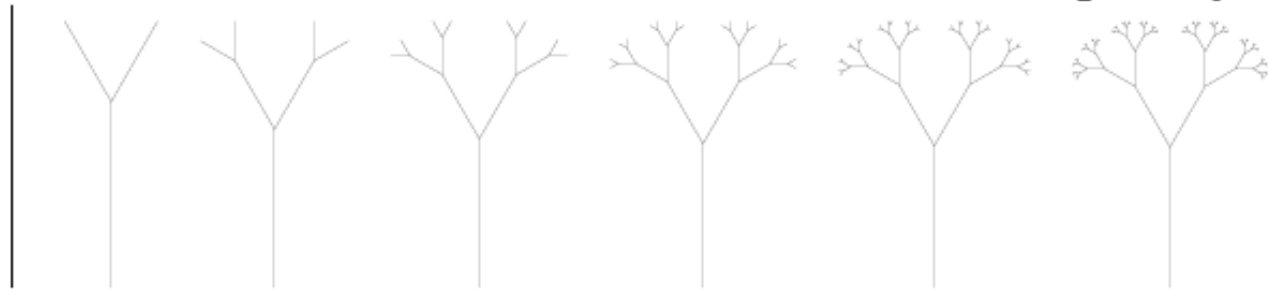


Koch Monopole

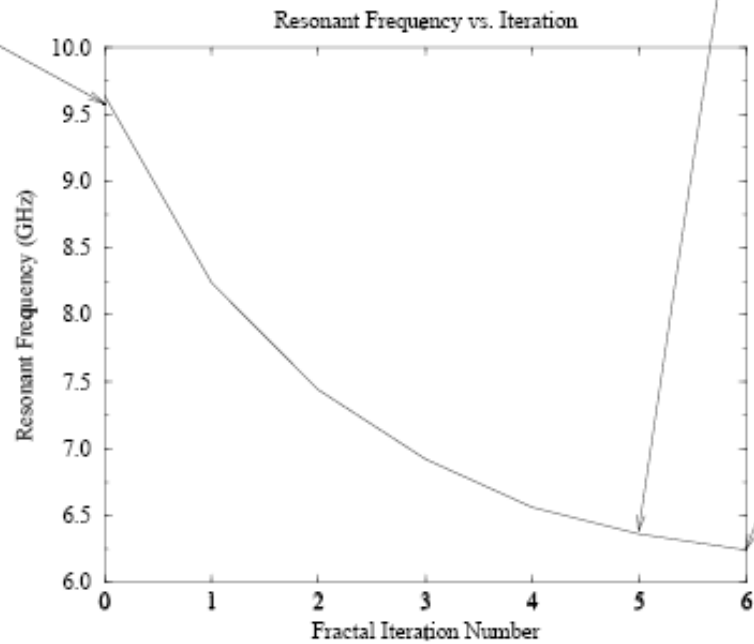
Length at Resonance versus Iteration



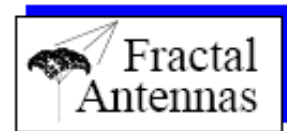
## Main Benefit: Decreased Resonant Frequency



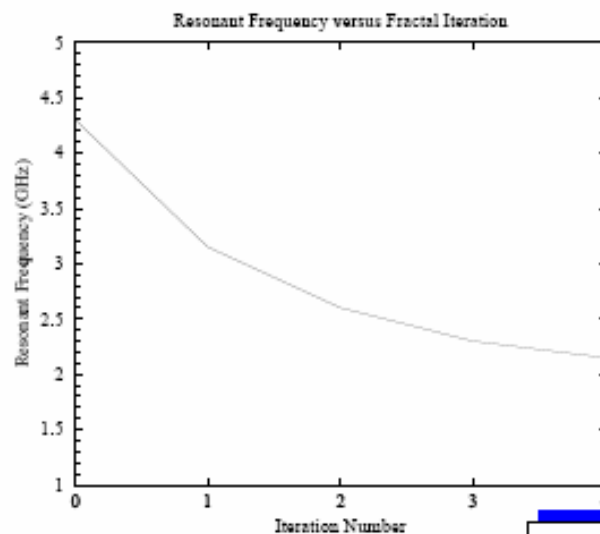
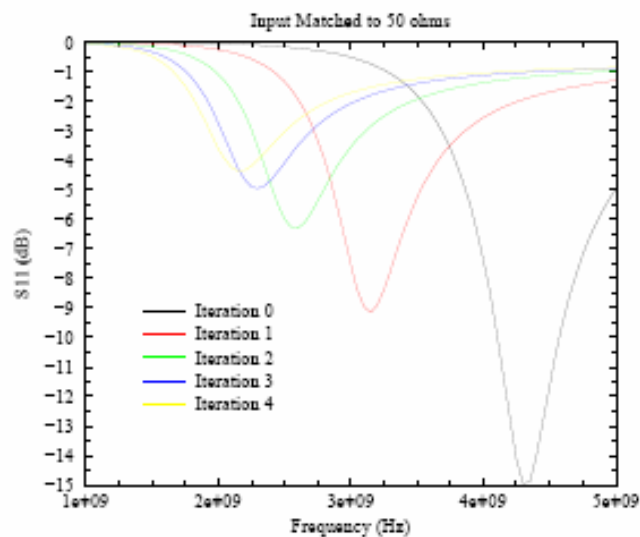
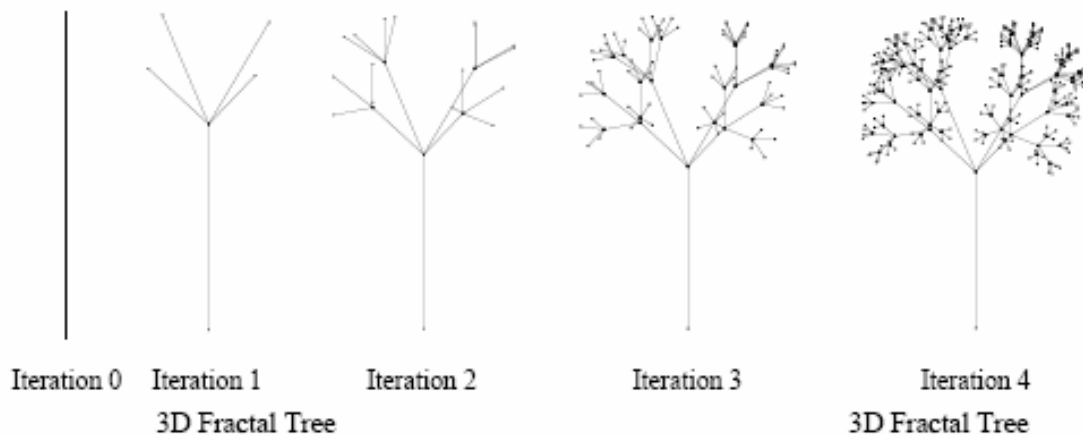
Fractal Tree Monopole over Ground Plane



Increasing Iteration  
Decreases Resonance



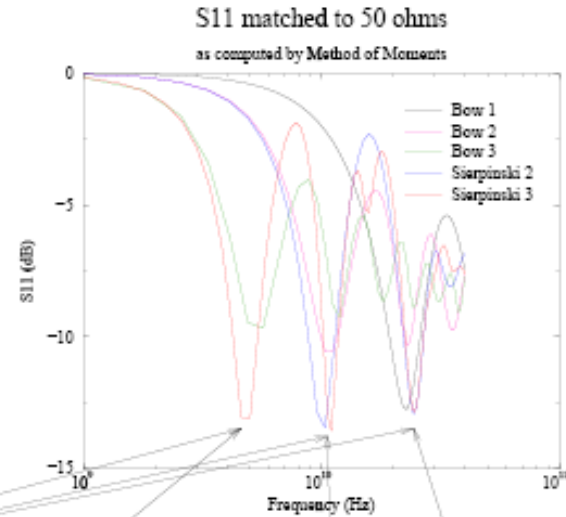
# Main Benefit: Decreased Resonant Frequency



# Sierpinski Sieve Dipole Antennas

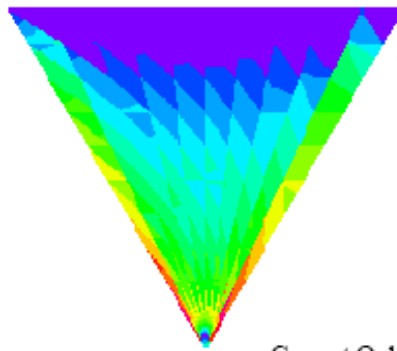
## Main Benefit: Multiband

The 3 bands matched by 3 different bowtie dipoles  
Are matched by 1 sierpinski dipole



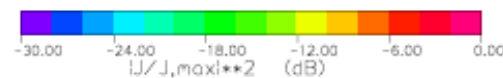
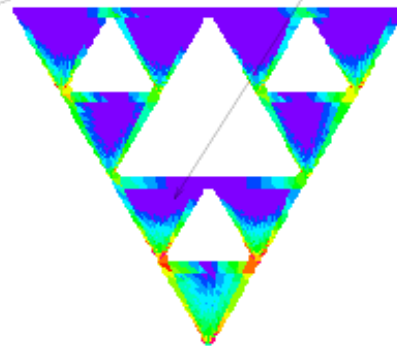
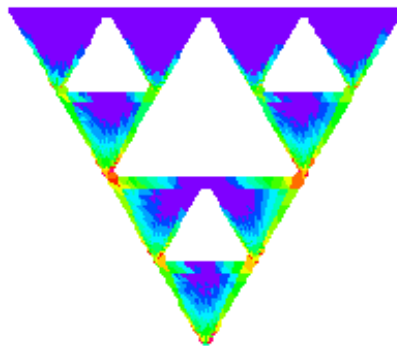
# Surface Currents Computed by Method of Moments

Surface Currents Clearly Show Multiband Behavior



Current at First Resonance Reaches to the Top of Bowtie Antenna

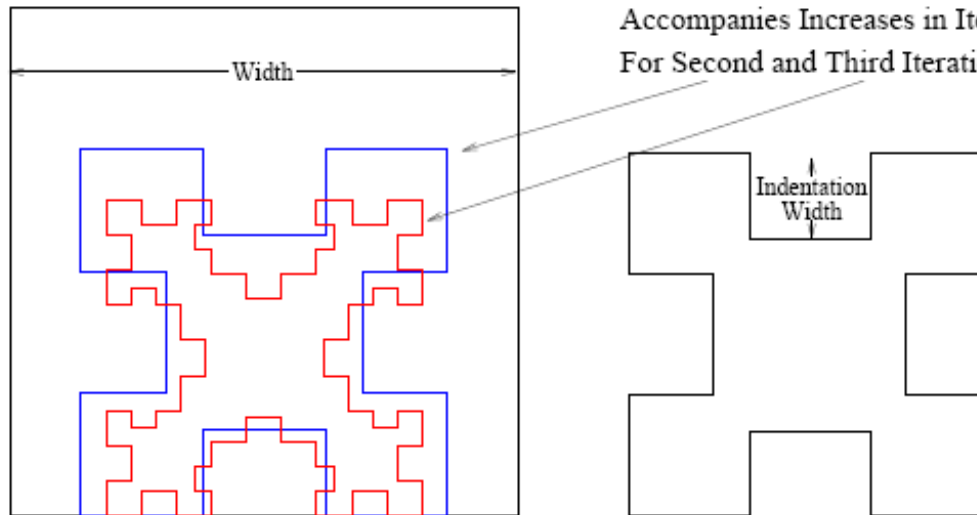
Current Only Sees Properly Scaled Antenna at First, Second, and Third Resonance



# Fractal Square Loop Antennas

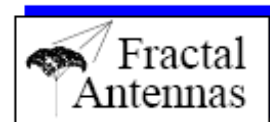
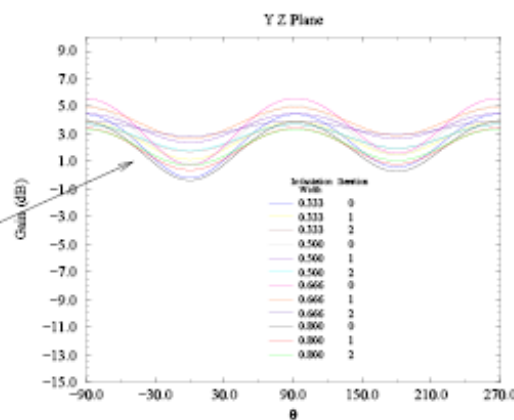
## Main Benefit: Decreased Size

Decreased Antenna Width  
Accompanies Increases in Iteration  
For Second and Third Iteration



Far Field Pattern

Far Field Pattern  
Remains Similar  
even with  
Smaller Area

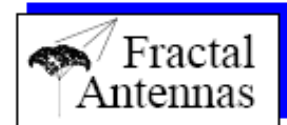
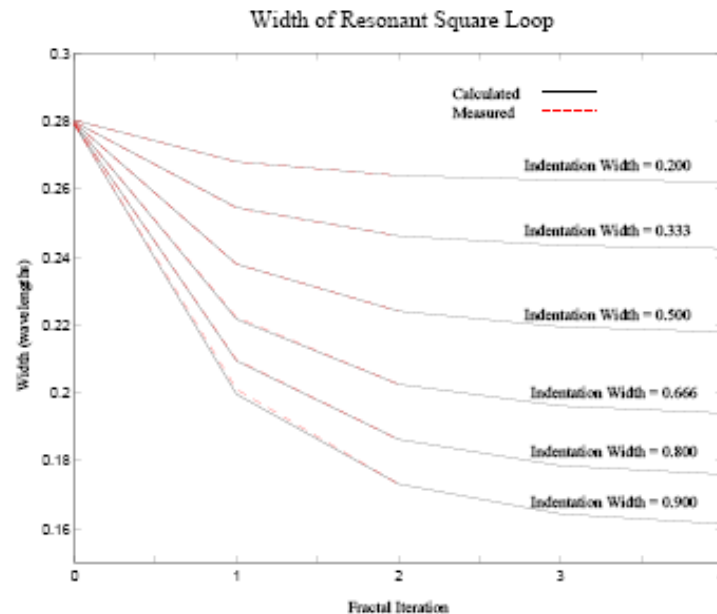


# Fractal Square Loop Antenna Design Curves

The Antenna can be Fabricated for a Given Iteration

$$Width = \frac{C}{e^{2^{n+1}} - 1}$$

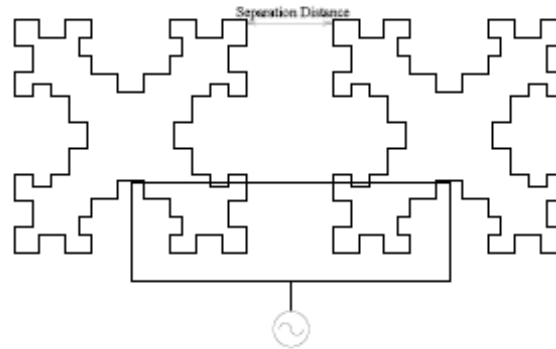
For a given indentation width,  
resonant loops can be designed  
using the above equation,  
where  $C$  is found empirically.



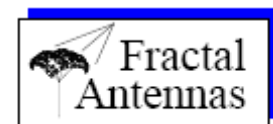
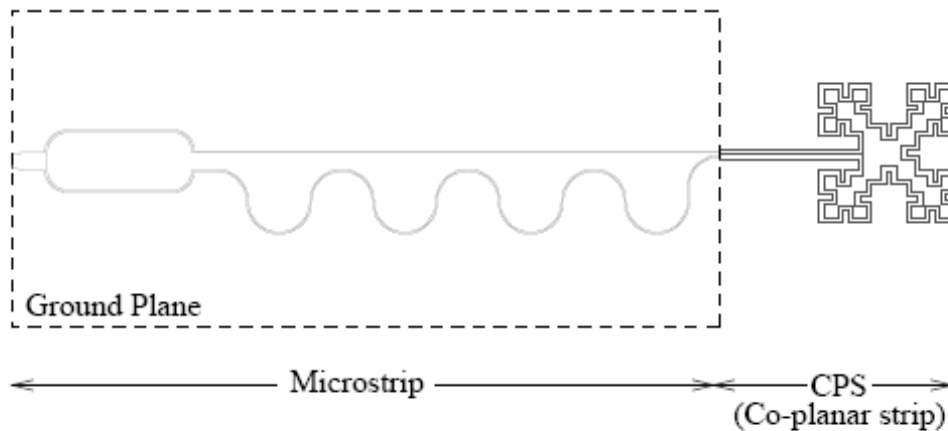
# Arrays with Fractal Elements

**Main Benefit: Decreases Mutual Coupling between Elements**

Separation Distance can be Maximized Using Fractal Elements



Thin Feeding Network for Fractal Array Elements



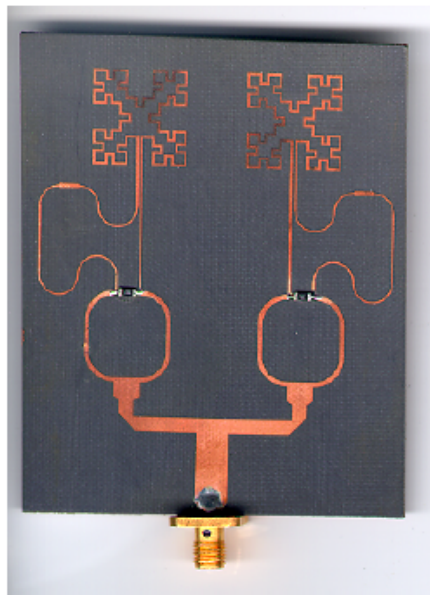


# John Gianvittorio - UCLA

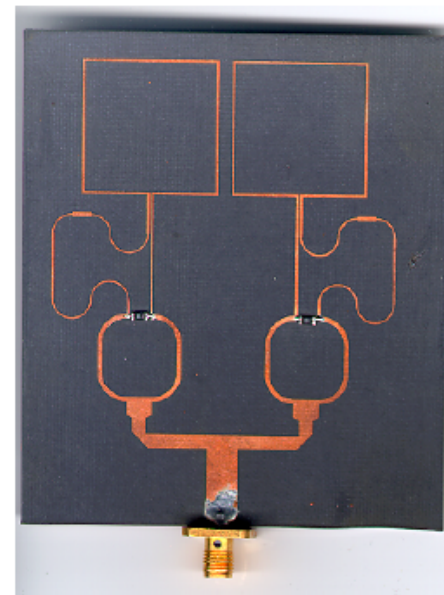
## Fabricated Fractal Array Antennas

---

Decreased inter-element coupling for fixed spacing  
Increased packing ability with smaller fractal elements



Fractal Array

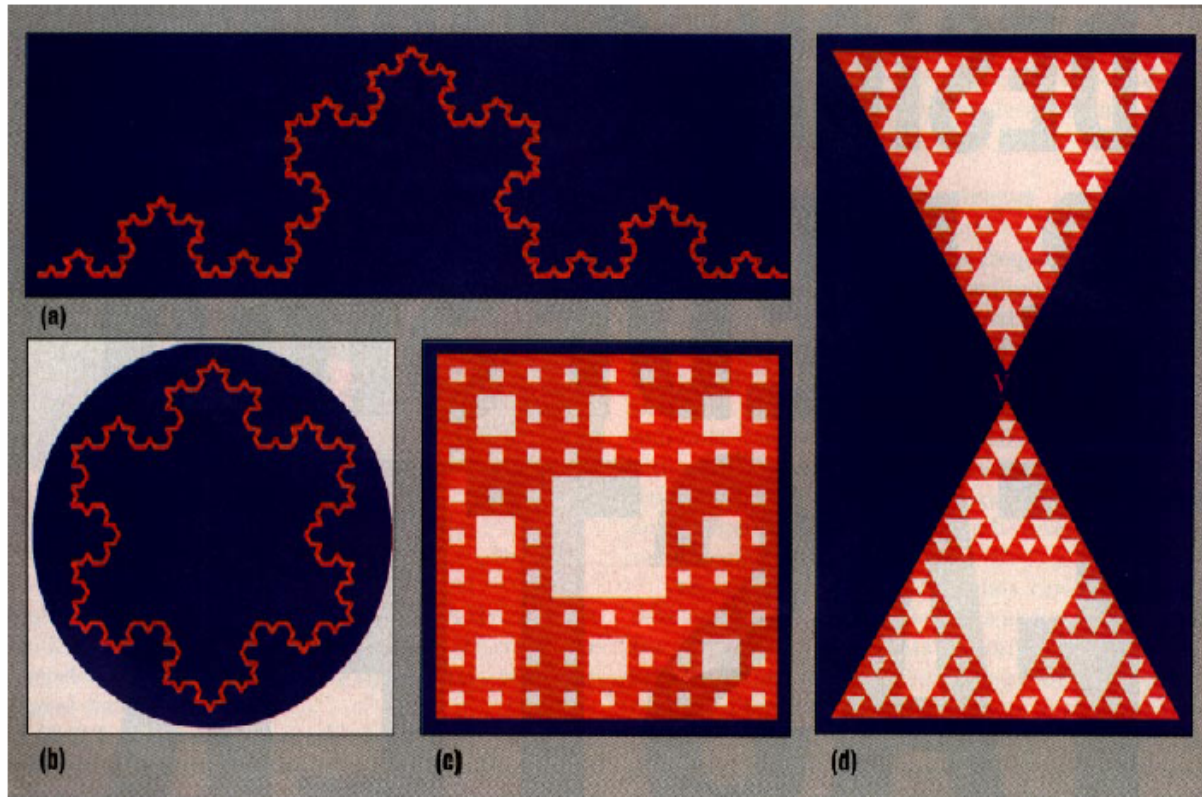


Standard Array

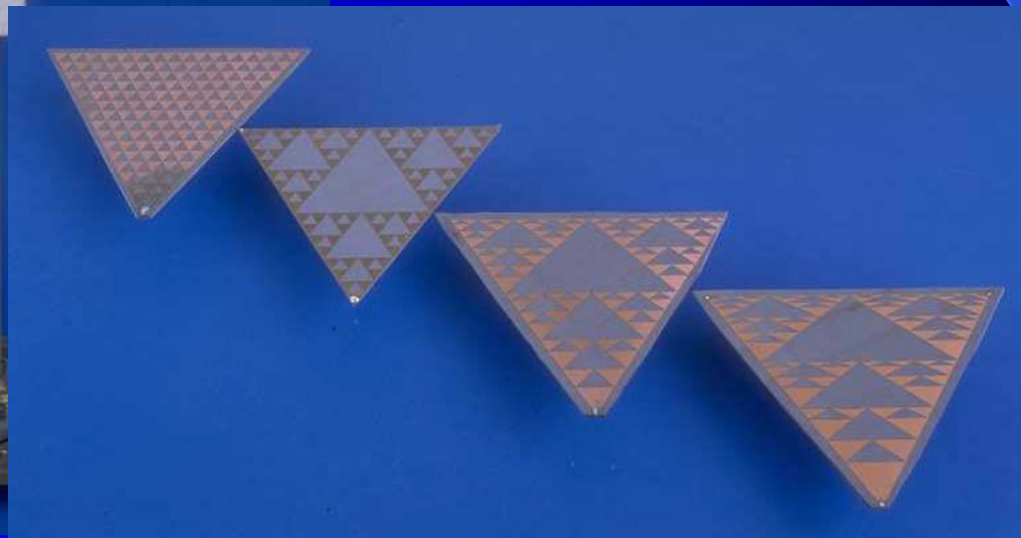
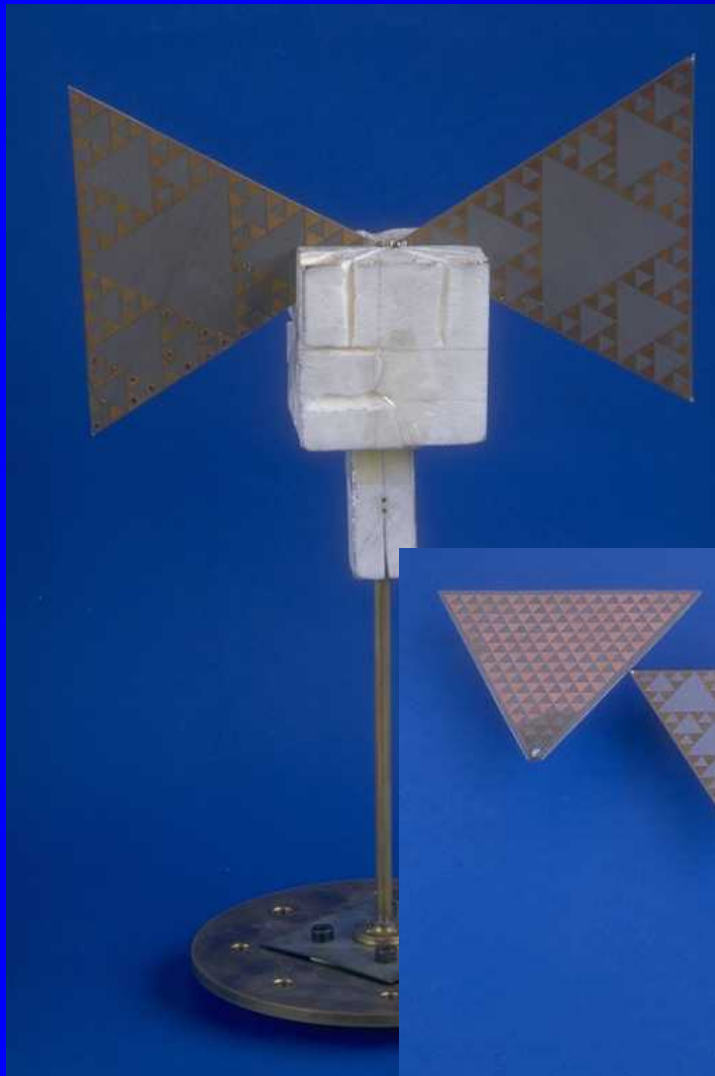


# Fractal antenna design

- Sample fractal antenna elements:

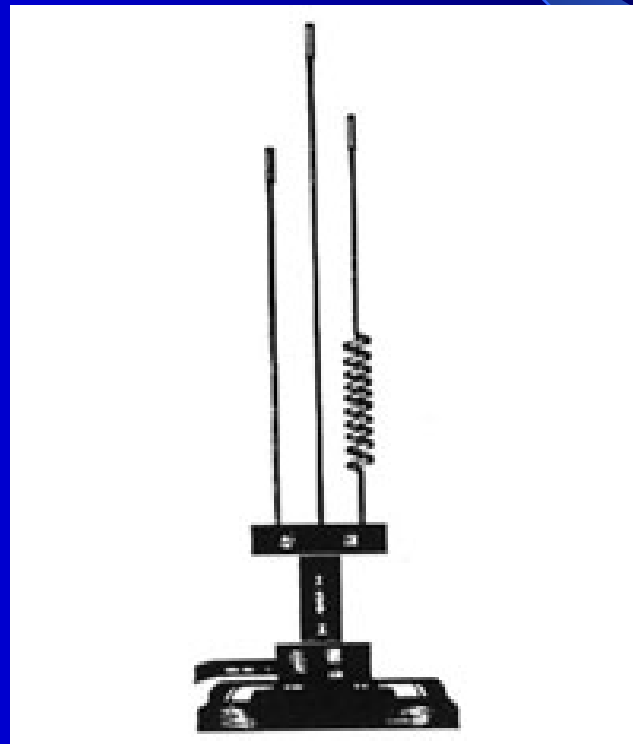


**(a)** Koch dipole    **(b)** Koch loop    **(c)** Cantor slot patch    **(d)** Sierpinski dipole



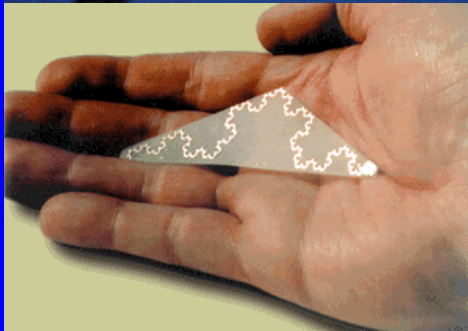
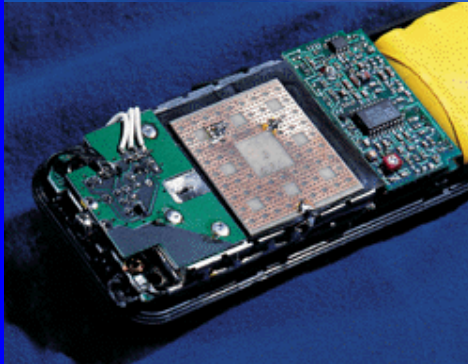
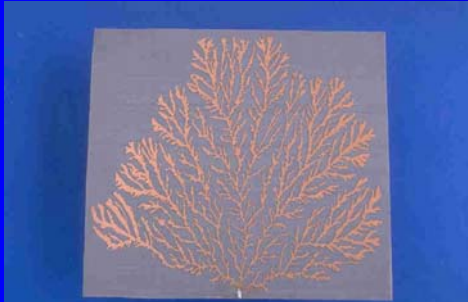
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August 18th, 2006

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Maciej J. Ogorzałek



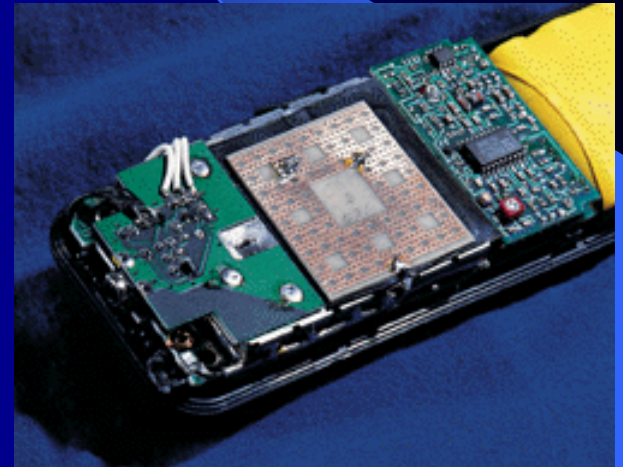
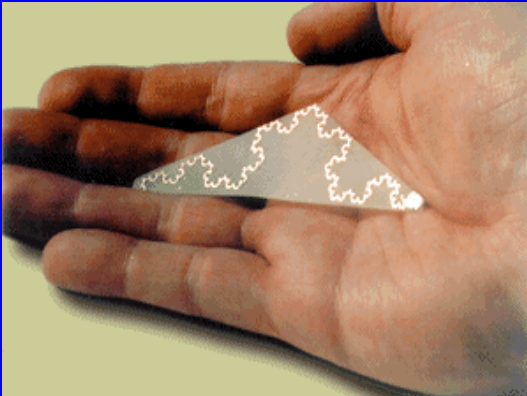
August 18th, 2006

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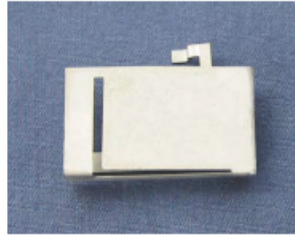
- Fractal antennas have superior multiband performance and are typically two-to-four times smaller than traditional aerials.
- Fractal antennas are the unique wideband enabler—one antenna replaces many.
- Multiband performance is at non-harmonic frequencies, and at higher frequencies the FEA is naturally broadband. Polarization and phasing of FEAs also are possible.

# Fractal Antenna

- Practical shrinkage of 2-4 times are realizable for acceptable performance.
- Smaller, but even better performance



## 900/1800/1900 MHz Tri-Band Antenna for GSM/DCS/PCS Wireless Applications



### Features

- *Efficient MLA Technology*
- *GSM/DCS/PCS Bands*
- *Peak Gain 0 dBi at 920 MHz*
- *Peak Gain 3 dBi at 1800 MHz*
- *Peak Gain 3 dBi at 1900 MHz*
- *Low Profile of less than 4.4 mm for Embedded Applications—1800 mm<sup>3</sup>*

This 900/1800/1900 MHz antenna is designed using SkyCross' patented MLA technology, providing superior efficiency and gain directivity in a small package. This antenna is the best performance solution for developers implementing a tri-band wireless system in the GSM, DCS and PCS bands where space is at a premium.

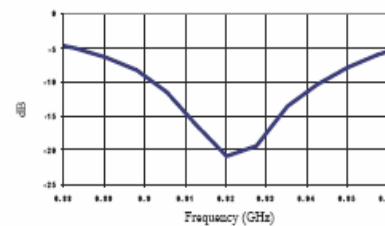
### Electrical Specifications

Frequency Range	880—960 MHz 1710—1880 MHz 1850-1990 MHz
Peak Gain	0 dBi at 920 MHz 3 dBi at 1800 MHz 3 dBi at 1900 MHz
VSWR	<3.5:1 GSM at band edges <3.5:1 DCS at band edges <2.5:1 PCS at band edges
Polarization	Linear
Azimuth Pattern	Omni-directional
Feed Impedance	50 Ohms Unbalanced

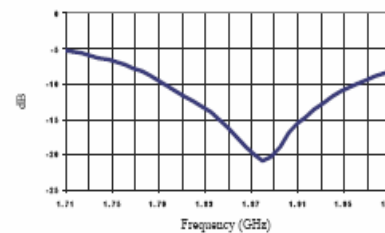
### Mechanical Specifications

Size	.97 x 0.51* x 0.17 inches 24.6 x 13.0* x 4.3 mm *width dimension does not include feed
Weight	0.8 g

### Low Band Return Loss



### High Band Return loss





# FRACTAL AND SPACE-FILLING TRANSMISSION LINES, RESONATORS, FILTERS AND PASSIVE NETWORK ELEMENTS

WO0154221

PUENTE BALIARDA CARLES [ES]; O'CALLAGHAN CASTELLA JUAN MANU [ES]; ROZAN EDOUARD JEAN LOUIS [ES]; COLLADO GOMEZ JUAN CARLOS [ES]; DUFFO UBEDA NURIA [ES]

FRACTUS S.A., Barcelona

This invention relates to high frequency electromagnetic circuits, in particular to those made on planar or quasi-planar substrates, where the circuit is patterned on a metallic or superconducting film on top of a dielectric in any of the configurations known to those skilled in the art (for instance micro-strip, strip-line, co-planar, parallel plate or slot-line configurations). A part of the circuit such as the characteristic strip or slot of said configurations is shaped in a novel space-filling or fractal geometry which allows a significant size reduction of the circuital component. Miniature transmission lines, capacitors, inductors, resistors, filters and oscillators can be manufactured this way.

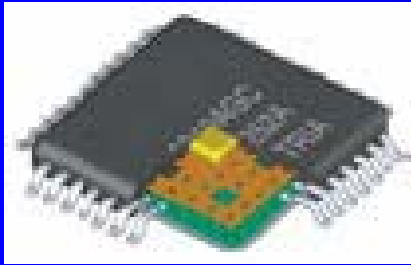
Also **NATHAN COHEN**, *CTO, Fractal Antenna Systems, Inc., 300 Commercial Street, Suite 27, Malden MA 02148 ; (617) 381-9595, FAX: (617) 489-6207. Fractal Antenna Website: <http://www.fractenna.com>.*

# Put the Antenna in the Package

The next major opportunity for wireless component manufacturers is to put the antenna into the package. Fractal-technology applied to antennas reaches the required miniaturisation to make Full Wireless System in Package (FWSiP) a reality.

FracWave™ technology

Fractus is the worldwide pioneer in the application of fractal geometries to antenna design and production. The space-filling properties of fractals enable the production of miniature antennas with optimal performance, and with multi-band capabilities. FracWave™ Antenna in Package (AiP) technology is suitable for Bluetooth®, WLAN, GPS, UWB and Zigbee and for sensors for automotive, biomedical and industrial purposes.



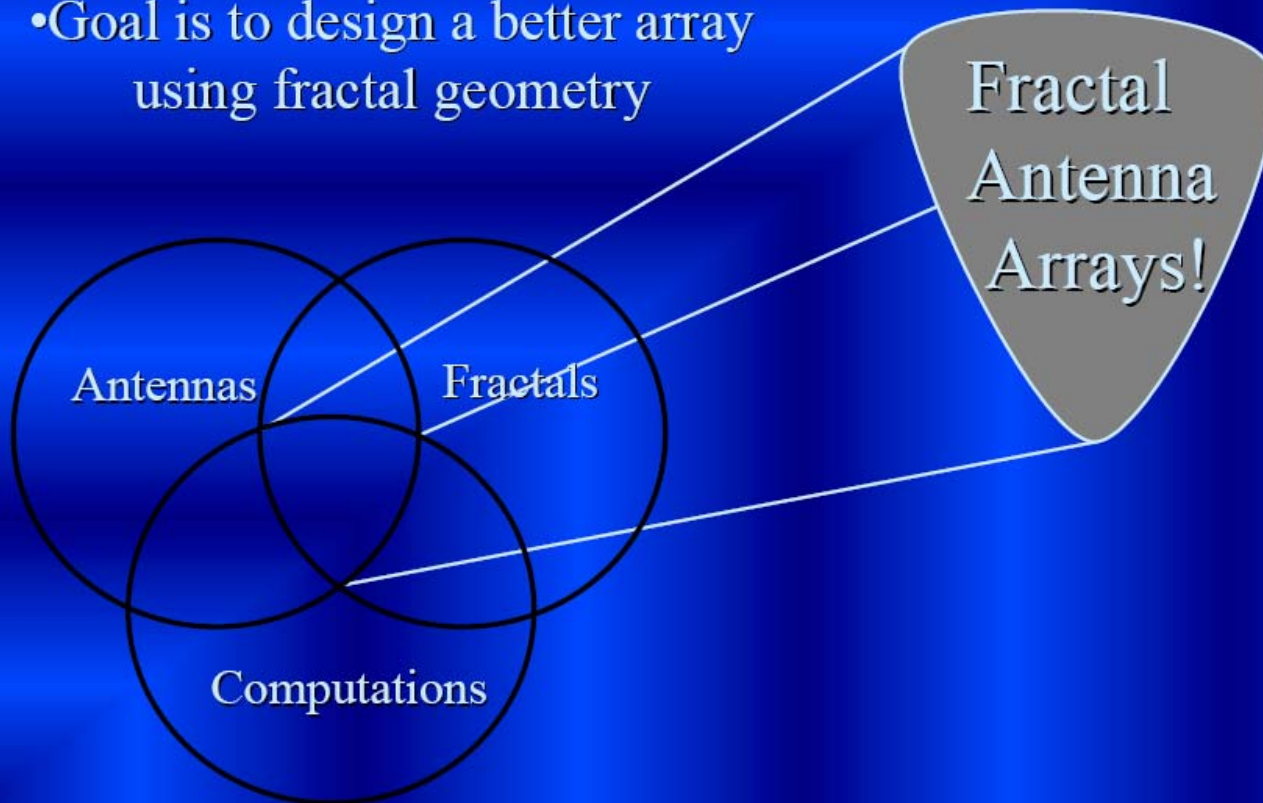
Visualization of antenna (the brown layer) integrated on a package substrate



AiP integrated on Bluetooth® adapter

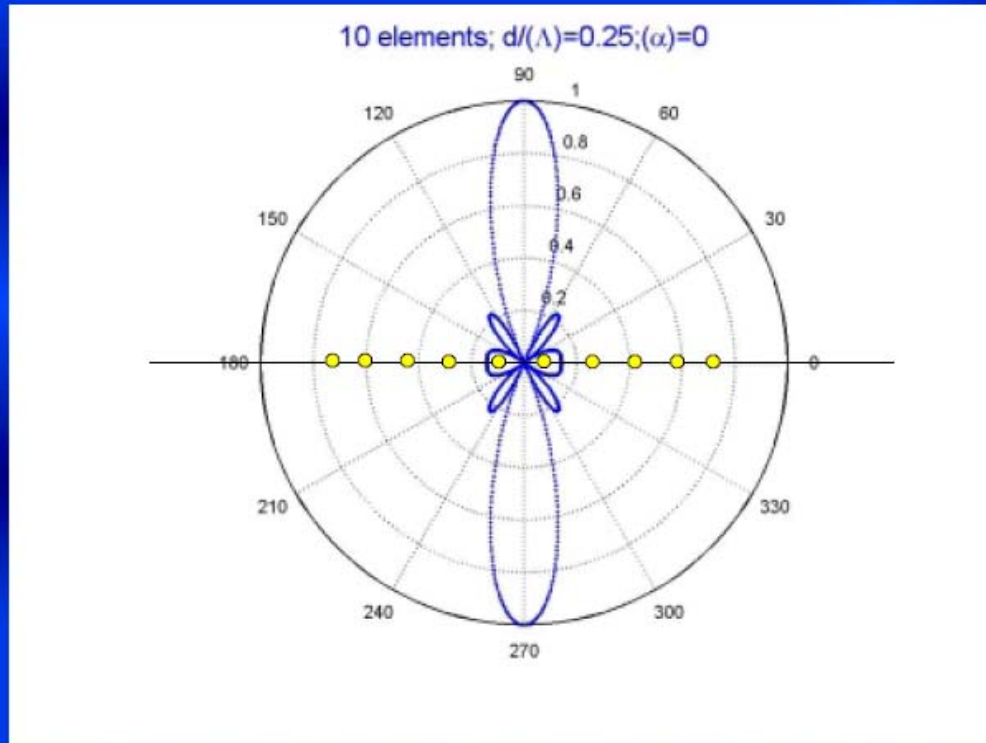
# “How does it all come together?”

- Goal is to design a better array using fractal geometry



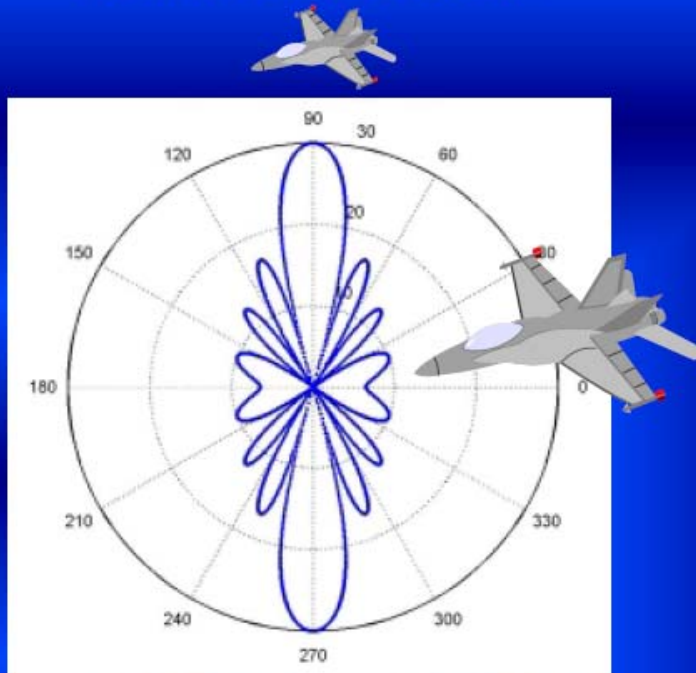
# Radiation

- Linear Antenna Array

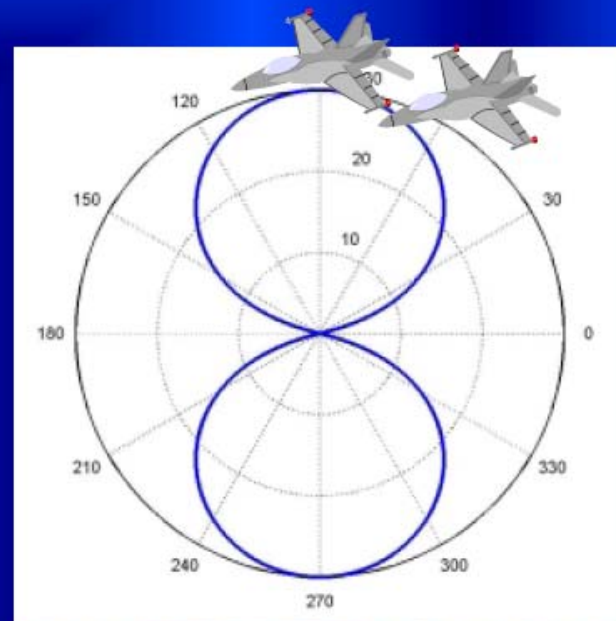


# An Ideal Array and Why

- Low/no side lobes

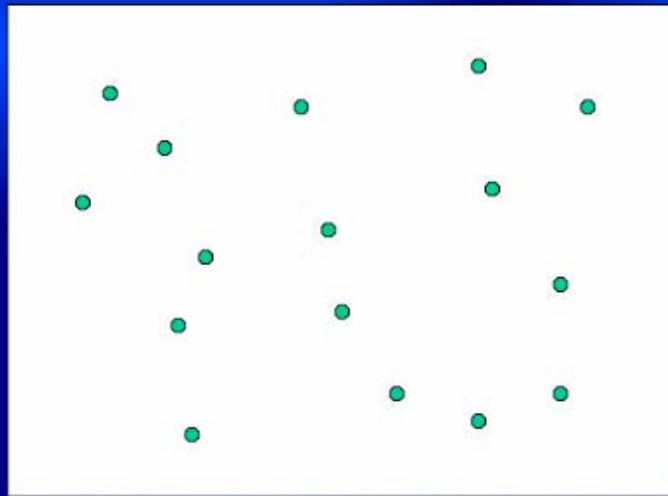


- Good quality main beam

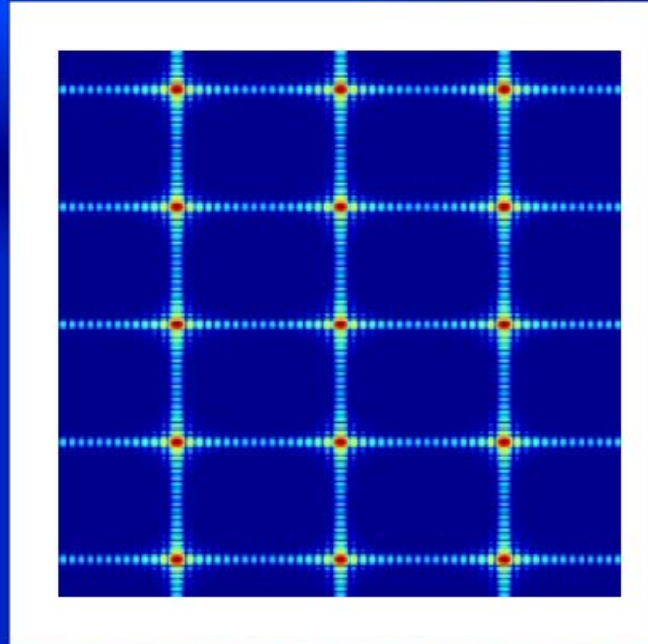
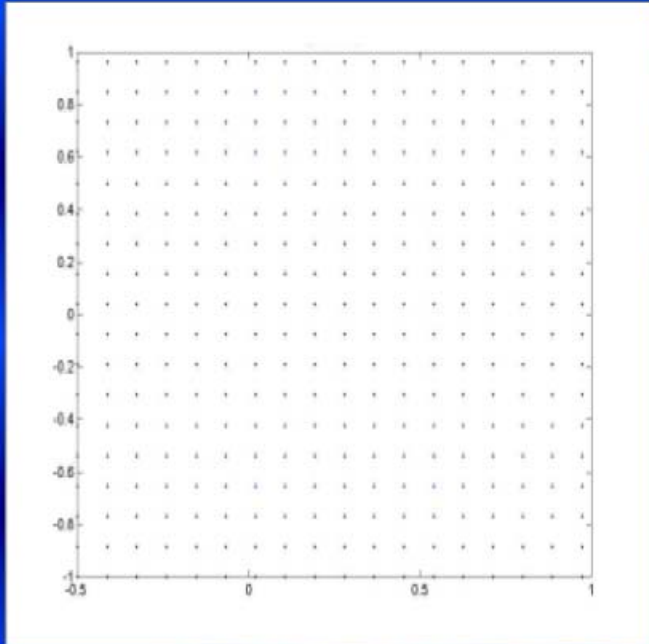


# More Radiation

- Periodic Array
- Random Array

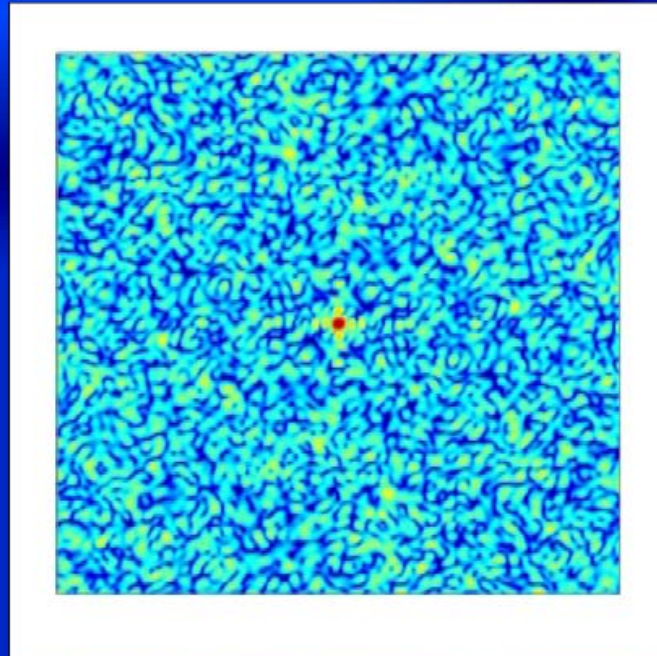
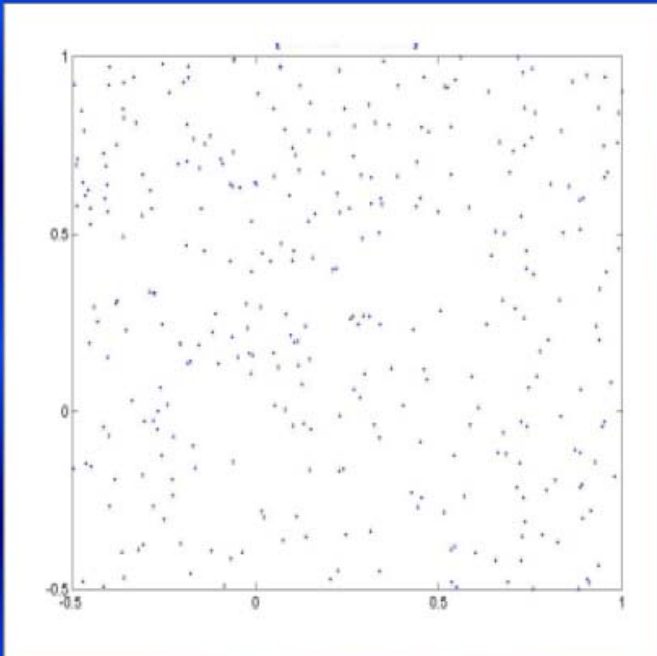


# Ordered Planar Array

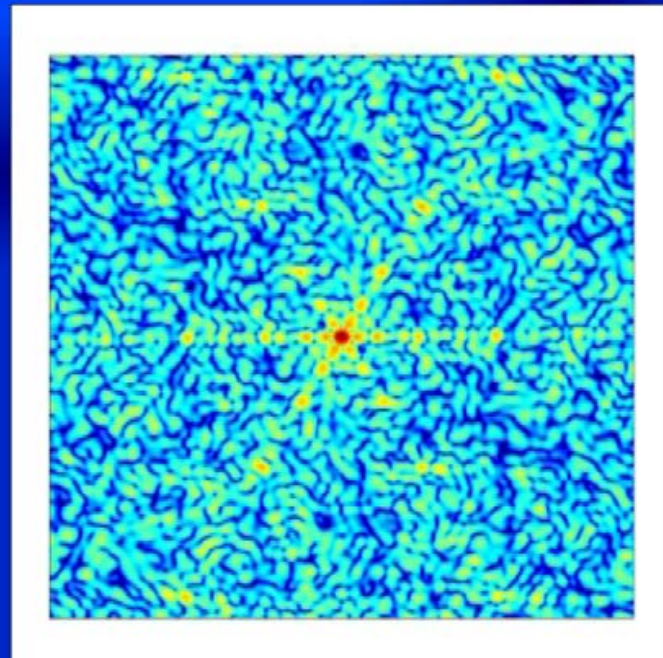
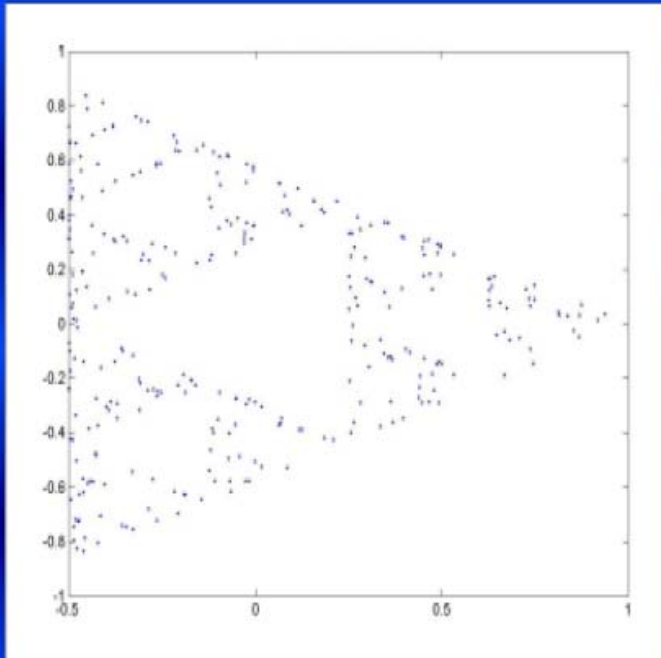




# Randomized Planar Array



# Fractal Planar Array

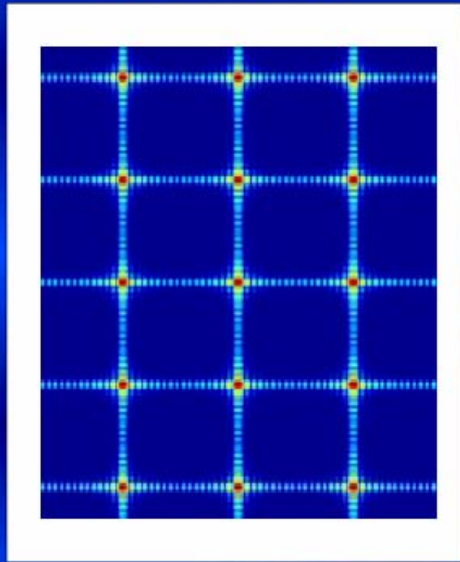


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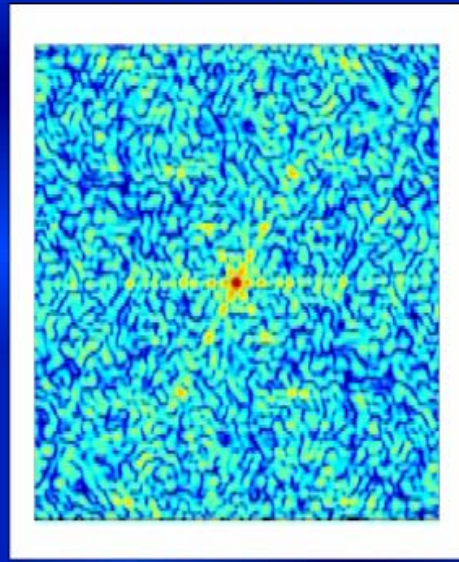
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# Comparison

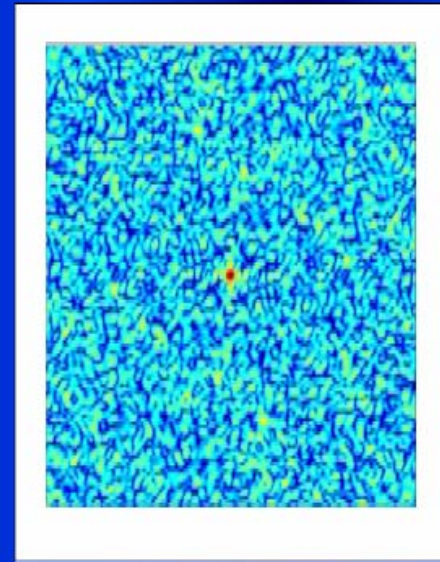
Periodic



Fractal



Random



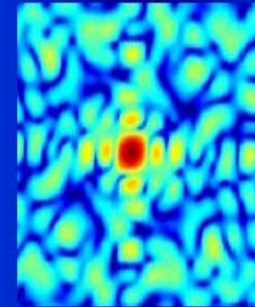
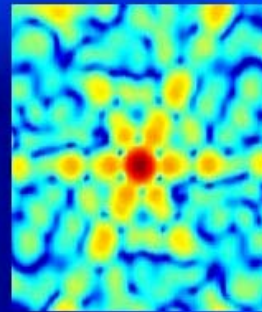
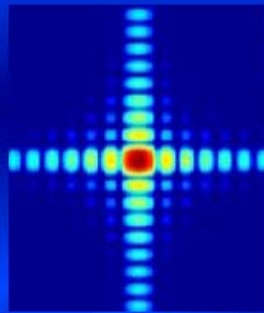
# Results

Periodic

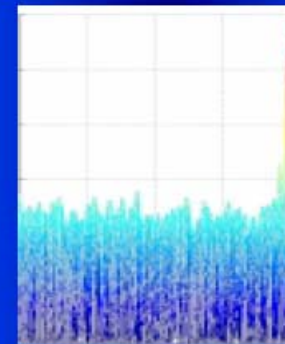
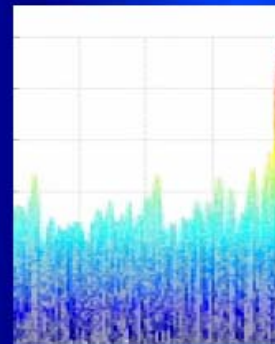
Fractal

Random

•Main beam



•Side lobes



## Fractus® Julia-12 ISM 2.4 GHz VPol

P/N: FR03-02-N-0-002

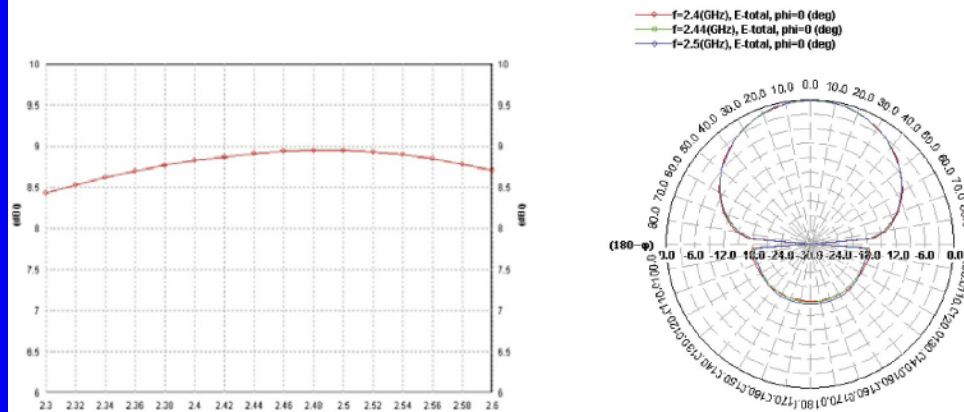
The JULIA-12 ISM 2.4 GHz panel antenna is a cost effective solution with an excellent broad coverage in a tiny package. The antenna features an internal Fractal shaped element and is suitable for both indoor and outdoor applications.



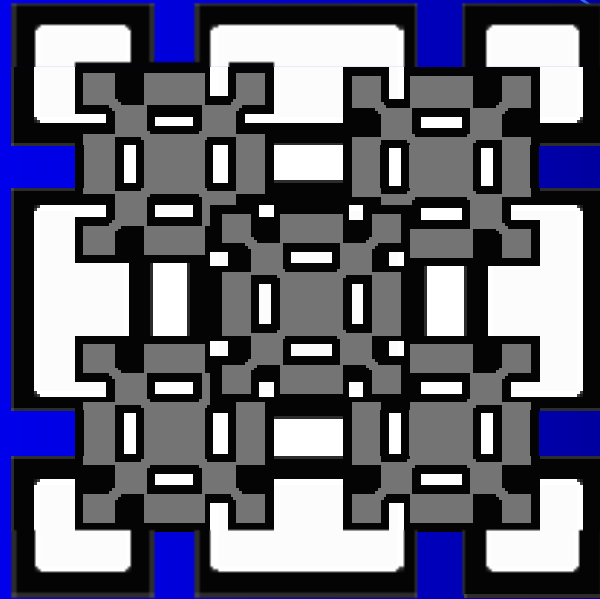
<b>Frequency Range</b>	2.4 - 2.5 GHz
<b>Directivity/Gain</b>	9.6 dBi / 8.8 dBi
<b>Impedance</b>	50 $\Omega$
<b>Polarisation</b>	VPOL
<b>F/B Ratio</b>	> 18 dB
<b>VSWR</b>	< 1.5 : 1
<b>Vertical Beamwith</b>	65°
<b>Horizontal Beamwith</b>	70°
<b>Connector (Pig Tail)</b>	RP-TNC or RP-SMA
<b>Radome</b>	ABS
<b>Dimensions</b>	10 x 10 x 3 cm

Measured results from a standard

Patent Pending: WO0154225, WO0122528,  
PCT/EP01/10589, PCT/EP02/07837, US60/613394,  
US60/627653 and PCT/EP02/07836



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## Fractus® Julia-10b ISM 2.4 GHz VPol

P/N: FR03-02-N-0-003

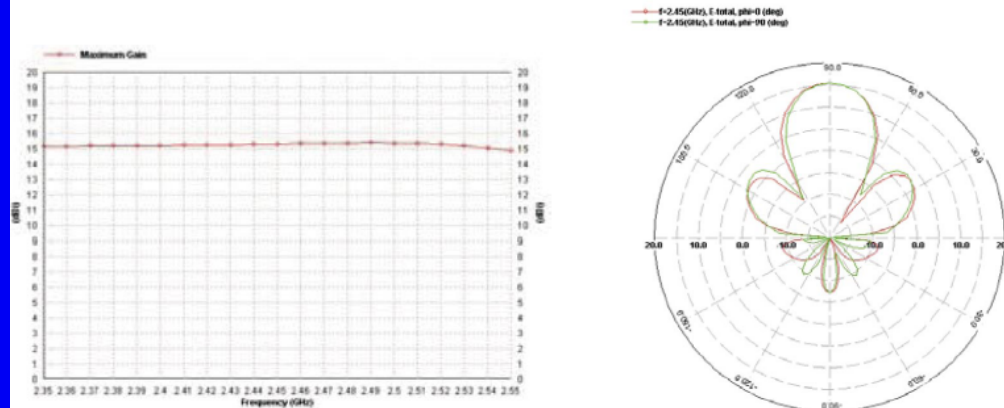
The **JULIA-10 ISM 2.4 GHz panel antenna** offers a superior gain to size ratio thanks to the Fractus' patented "Super Directive" patch design. JULIA-10 is the ideal choice to get extra range capacity in a tiny package.



<b>Frequency Range</b>	2.4 - 2.5 GHz
<b>Directivity/Gain</b>	16 dBi / 15 dBi
<b>Impedance</b>	50 $\Omega$
<b>Polarisation</b>	VPOL
<b>F/B Ratio</b>	> 20 dB
<b>VSWR</b>	< 1.5 : 1
<b>Vertical Beamwith</b>	30°
<b>Horizontal Beamwith</b>	35°
<b>Connector (Pig Tail)</b>	RP-TNC or RP-SMA
<b>Radome</b>	ABS
<b>Dimensions</b>	21 x 21 x 3 cm

Measured results from a standard

Patent Pending: WO0154225, WO0122528,  
PCT/EP01/10589, PCT/EP02/07837, US60/613394,  
US60/627653 and PCT/EP02/07836



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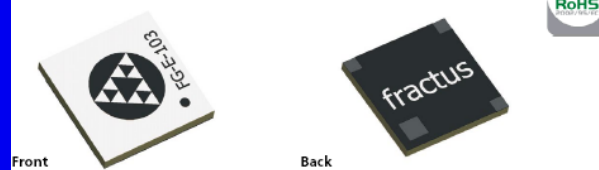
## Fractal Geofind™ GPS Slim Chip Antenna

P/N: FR05-S1-E-0-103

The **Fractal Geofind** is an slim chip antenna engineered specifically for consumer electronic devices operating with GPS system where low-cost and robust performance is mandatory.

Taking advantage of the space-filling properties of fractals, this **small planar monopole** antenna is ideal for use low-cost consumer electronic devices to add personal location functionalities. The **Fractal Geofind GPS Slim Chip Antenna** speeds your time-to-market by allowing you to integrate it within your industrial design easily (SMD mounting) and efficiently.

10 x 10 x 0.9 mm (image larger than actual size)



Patent Pending: WO0154225, WO0122528, PCT/EP01/10589, PCT/EP02/07837, US60/613394, US60/627653 and PCT/EP02/07836

### Product Benefits

#### ■ High performance/price ratio

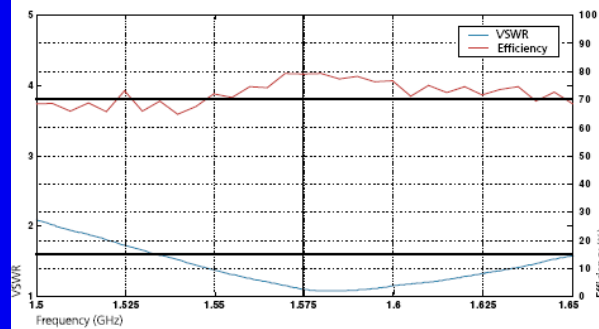
Raises your device's competitiveness by increasing satellite sensitivity and decreasing your device's BoM cost.

#### ■ Omnidirectional pattern

Optimises device usage due to a uniform radiation pattern.

#### ■ Small Volume

Allows integration into space limited areas easily and efficiently.



Frequency Range	1575 MHz
Efficiency	> 70 %
Peak Gain	> 1 dBi
VSWR	< 1.6:1
Weight	0.20 g
Temperature	-40 to +85 °C
Impedance	50 Ω unbalanced
Dimensions	10 x 10 x 0.9 mm

Measured results from a standard PCB of 70x30 mm

Please contact your sales representative at Richardson Electronics to obtain additional information on recommended configurations for different UWB devices. Richardson Electronics: [www.rell.com](http://www.rell.com) Fractus: [wireless@fractus.com](mailto:wireless@fractus.com) Reference: DS\_FR05-S1-E-0-103\_v01

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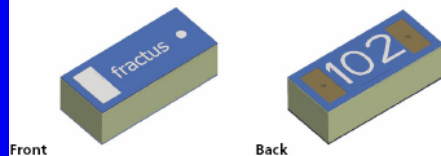
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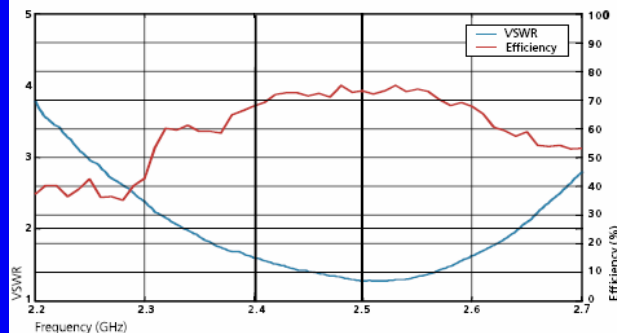
The **Fractus Compact Reach Xtend Chip Antenna** for Bluetooth® and 802.11 b/g WLAN is a tiny rectangular 3D-shaped antenna suitable for headset, compact flash (CF), secure digital (SD) and other small PCB devices operating at 2.4 GHz where high performance and low-cost are mandatory. Its broad bandwidth ensures high quality signal reception and transmission across wireless devices and different plastic housing designs.

Taking advantage of the space-filling properties of fractals, this **small monopole** antenna is ideal for use within indoor (highly scattered) environments. The **Fractus Compact Reach Xtend Chip Antenna** speeds your time to market by allowing you to easily integrate it within your industrial design (SMD mounting).

7 x 3 x 2 mm (image larger than actual size)



**Patent Pending:** WO0154225, WO0122528, PCT/EP01/10589, PCT/EP02/07837, US60/613394, US60/627653 and PCT/EP02/07836



## Product Benefits

### ■ Small form factor

Allows integration into space limited areas easily and efficiently with minimum clearance area.

### ■ Broad bandwidth

Ensures robust performance when considering different plastic housing and close body proximity.

### ■ Omnidirectional pattern

Optimises device usage due to a uniform radiation pattern.

### ■ Multi-mode support

Works for Bluetooth, and Wi-Fi 802.11b and g standards.

<b>Frequency Range</b>	2.4 - 2.5 GHz
<b>Efficiency</b>	> 70 %
<b>Peak Gain</b>	> 1 dBi
<b>VSWR</b>	< 2:1
<b>Weight</b>	0.20 g
<b>Temperature</b>	-40 to +85 °C
<b>Impedance</b>	50 Ω unbalanced
<b>Dimensions</b>	10 x 10 x 0.8 mm

Measured results from a standard PCB of 47x23 mm

Please contact your sales representative at Richardson Electronics to obtain additional information on recommended configurations for different UWB devices. Richardson Electronics: [www.rell.com](http://www.rell.com) Fractus: [wireless@fractus.com](mailto:wireless@fractus.com) Reference: DS\_FR05-S1-N-0-102\_v01

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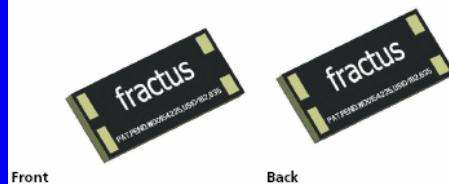
## Fractus® EZConnect™ Zigbee™ Chip Antenna

P/N: FR05-S1-R-0-105

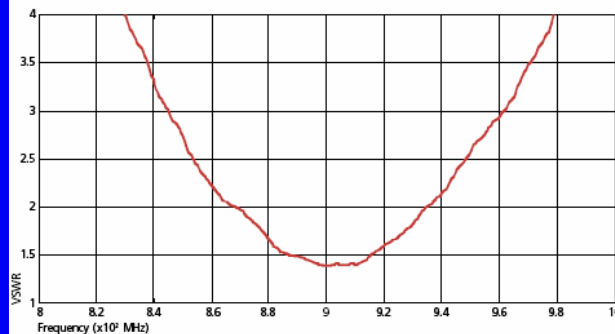
The Fractus **EZConnect Zigbee Chip Antenna** is a compact rectangular antenna suitable for smart home, security and other industrial devices using the 915 MHz ISM band, where low power consumption and cost are top of mind. Taking advantage of the space-filling properties of fractals, this **compact monopole** antenna is ideal for use within indoor (highly scattered) as well as outdoor environments.

The **Fractus EZConnect Zigbee Chip Antenna** speeds your time to market by allowing you to easily integrate it within your industrial design (SMD mounting).

18 x 7,3 x 1 mm (image larger than actual size)



**Patent Pending:** WO0154225, WO0122528, PCT/EP01/10589, PCT/EP02/07837, US60/613394, US60/627653 and PCT/EP02/07836



### Product Benefits

#### ■ Small form factor

Allows integration into space limited areas easily and effectively.

#### ■ Broad bandwidth

Ensures robust performance in different PCB dimensions and plastic housing, without the need for a matching network.

#### ■ High performance

Optimises power consumption and increases device range.

#### ■ Omnidirectional pattern

Increases device robustness due to a uniform radiation pattern.

**Frequency Range** 902 - 928 MHz

**Efficiency** > 40 %

**Peak Gain** > 0 dBi

**VSWR** < 2:1

**Weight** 0.20 g

**Temperature** -40 to +85 °C

**Impedance** 50 Ω unbalanced

**Dimensions** 18 x 7,3 x 1 mm

Measured results from a standard PCB of 120x65 mm

Please contact your sales representative at Richardson Electronics to obtain additional information on recommended configurations for different UWB devices. Richardson Electronics: [www.rell.com](http://www.rell.com) Fractus: [wireless@fractus.com](mailto:wireless@fractus.com) Reference: DS\_FR05-S1-E-0-105\_v01

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*Customised Mobile Handset Antenna  
Pat. Pending: WO012258, VS2002140615,  
WO0154225, VS10/182,635*



*Fractus Compact Dual-Band Reach Xtend™  
WLAM 802.11 a/b/g/j/n Chip Antenna 2.4 & 5GHz*

## ELECTRONIC WARFARE



### UAB™ Antenna

Extreme wideband and omnidirectional performance with superior gain. Operates with or without a ground plane over a 25:1 frequency range, from VHF to microwave. Compact form factor packaged in a 7.7 inch-diameter, 10 inch-high radome weighing 4.8 pounds. Up to 250W input power. VSWR less than 2:1.



### UAD™ Antenna

Extreme wideband performance with up to 250W power handling and superior gain. Operates over UHF to microwave. Low profile of 5.7 inches and easily concealable in a 7.7 inch-diameter radome. VSWR less than 2:1.



### UGS™ Antenna

Single antenna integrated with an unattended ground sensor (UGS) providing superior omnidirectional long-range performance. Operates over high HF through VHF. Innovative raised phase center design minimizes ground losses, while improving radiation pattern and launch angle. Easily deployed in a compact, lightweight package measuring 2.5 inches in diameter and 3 feet in height.



### RFsabre™

With outstanding lower frequency gain and less than 3:1 VSWR over a very wide frequency range, the RFSabre antenna delivers great performance in a distinctly compact form factor. The vehicle-mounted version can survive impacts with solid objects at speeds up to 25 MPH. Geared for security, communications, signal gathering, and high power transmit applications. New hanging or tripod mounted versions available.



Fractal antenna technology, implemented in transparent conductive film, makes covert capability possible with a mission-capable antenna system that operates over a huge frequency range.

- Outstanding gain
- Transparent
- Conformable
- Only 13 x 18 inches
- VSWR less than 3:1
- Inherently 50 Ohms
- Optional frequency lowering panels

Signal intelligence warfighters face a difficult challenge — the need to monitor communications over a very wide frequency range while remaining clandestine. Current electronic surveillance systems employ multiple antennas that are either large or noisy. Covertness and high performance are united in the Tranztenna™ optically transparent antenna: an extremely wideband antenna designed for vehicle or building window placement. This conformable, rugged, compact antenna is easy to transport and install in field operations. New missions to intercept and monitor enemy communications are possible with this breakthrough in transparent antenna technology.

Feature	Advantage	Benefit
Transparent	Visually unobtrusive	Covert use of antenna in vehicle or building window
Good Gain	Superior to ITO films	Excellent signal-to-noise ratio
Wideband	Operation over very wide frequency range	Instantaneously access most spectrum of interest
Compact Size	Effective use of small window apertures	Access to lower frequencies
Conformable	Flexible sheet	Easy transport and deployment

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